Prof. R.A. Serota Quiz 4

Name _____

Useful formulae:

$$R = \rho \frac{L}{A}$$

$$I = \frac{\mathcal{E}}{R}$$

$$R_{eq} = \sum_{j=1}^{n} R_j$$
 (*n* resistances in series)

$$\frac{1}{R_{eq}} = \sum_{j=1}^{n} \frac{1}{R_j}$$
 (*n* resistances in parallel)

1. A certain wire has a resistance R. What is the resistance of a second wire, made of the same material that is half as long and has half the diameter?

Solution

In terms of resistivity ρ , which is the same for both wires,

$$R_1 = \rho \frac{L_1}{A_1} = R$$

and

$$R_2 = \rho \frac{L_2}{A_2}$$

whereof

$$\frac{R_2}{R} = \frac{L_2 A_1}{L_1 A_2} = \frac{L_2 D_1^2}{L_1 D_2^2} = \frac{L_2}{L_1} \left(\frac{D_1}{D_2}\right)^2 = 2$$

That is

$$R_2 = 2R$$

2. Four 18.0 Ω resistors are connected in parallel across a 25.0 V ideal battery. What is the current across the battery?

Solution

The equivalent resistance is

$$R_{eq} = \frac{18.0}{4} = 4.5 \ \Omega$$

and

$$I = \frac{\mathcal{E}}{R_{eq}} = \frac{25.0 \text{ V}}{4.5 \Omega} = 5.56 \text{ A}$$

3. The current in a single-loop circuit with one resistance R is 5.0 A. When an additional resistance of 2.0 Ω is inserted in series with R, the current drops to 4.0 A. What is R?

Solution

For emf \mathcal{E} , the current is

$$I_i = \frac{\mathcal{E}}{R} = 5.0$$

initially, and is

$$I_f = \frac{\mathcal{E}}{R+2} = 4.0$$

after the additional resistance is inserted. Combining the two equations, we find

$$\frac{R+2}{R}=\frac{5.0}{4.0}$$

whereof

$$R = 8.0 \Omega$$