

Syllabus
 Symbolic Logic II
 Winter Quarter, 2010-2011
 Professor John Martin

Textbook *Introduction to Metalogic*

http://homepages.uc.edu/~martinj/Symbolic_Logic/342%20Syllabus,%20Textbook,%20Handouts,%20Notes/

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Course grading will be based on exercises and quizzes as necessary.

The instructor reserves the right to alter the syllabus as necessary.