

Examples of the (nested) Semantic Properties Necessity, Impossibility, Validity, and Equivalence that depend on the meaning of:

(1) just the Sentential Connectives ($\neg, \wedge, \vee, \rightarrow$),

(2) the Sentential Connectives and the symbols of First-Order Logic (FOL) ($\neg, \wedge, \vee, \rightarrow$ plus $=, \forall, \exists$), and

(3) the Sentential Connectives, the symbols of First-Order Logic, and descriptive terms (constants and predicates) ($\neg, \wedge, \vee, \rightarrow, =, \forall, \exists$ plus *LeftOf, RightOf, Cube, Tet, Dodec, Small, Large, Larger, SameSize*)

	Necessary formulas, sentences	Impossible formulas, sentences	Valid arguments	Equivalent pairs of formulas, sentences
Depending on: $\neg, \wedge, \vee, \rightarrow$ ("sentential", "propositional" "Tautological")	$A \vee \neg A$ $A \rightarrow A$ $(A \wedge B) \rightarrow B$ (Tautologies)	$A \wedge \neg A$ $\neg(A \rightarrow A)$ $\neg(A \vee \neg A)$	$A \wedge B / \therefore A$ $A, A \rightarrow B / \therefore B$ $A \vee B, \neg B / \therefore A$ (Tautological Consequences)	$A \wedge B :: B \wedge A$ $A \rightarrow B :: \neg A \vee B$ $\neg(A \wedge B) :: \neg A \vee \neg B$ (Tautological Equivalents)
Depending on: $=, \forall, \exists$ ("formal", "logical", "first-order")	$c=c$ $\forall x \exists y (x=y)$ $\forall x F(x) \rightarrow \exists x F(x)$ $\forall x (F(x) \vee \neg F(x))$ (FOL truths)	$c \neq c$ $\forall x F(x) \wedge \neg \exists x F(x)$ $\neg \exists x (x=x)$ $\exists x (F(x) \wedge \neg F(x))$	$a=b, F(a) / \therefore F(b)$ $\forall x (F(x) \wedge G(x)) / \therefore \exists x F(x)$ $\exists x F(x) / \therefore \exists x (F(x) \vee G(x))$ $\forall x (F(x) \rightarrow G(x)), \exists x F(x) / \therefore \exists x G(x)$ (FOL Consequences)	$\neg \forall x F(x) :: \exists x \neg F(x)$ $\neg \exists x F(x) :: \forall x \neg F(x)$ $\neg \exists x (F(x) \wedge G(x)) :: \forall x (F(x) \rightarrow \neg G(x))$ $\neg \forall x (F(x) \rightarrow G(x)) :: \exists x (F(x) \wedge \neg G(x))$ (FOL Equivalents)
Depending on: Constants, Predicates ("descriptive", "analytic")	$\text{LeftOf}(x,y) \rightarrow \text{RightOf}(y,x)$ $a=b \rightarrow \text{SameSize}(a,b)$ $\text{Cube}(x) \vee \text{Tet}(x) \vee \text{Dodec}(x)$ (Analytic Truths)	$\text{Cube}(x) \wedge \text{Tet}(x)$ $\text{LeftOf}(x,x)$ $\text{Small}(x) \wedge \text{Large}(x)$ (Analytic Impossibilities)	$\text{Cube}(x) / \therefore \neg \text{Tet}(x)$ $\text{LeftOf}(x,y), \text{LeftOf}(y,z) / \therefore \text{LeftOf}(x,z)$ $\text{Small}(x), \text{Large}(y) / \therefore \text{Larger}(y,x)$ (Analytic Consequences)	$\text{LeftOf}(x,y) :: \text{RightOf}(y,x)$ $\text{Cube}(x) :: \neg(\text{Tet}(x) \wedge \text{Dodec}(x))$ $\text{SameSize}(x,y) :: \neg(\text{Larger}(x,y) \wedge \text{Smaller}(x,y))$ (Analytic Equivalents)