

Sides of "The" Unitarity Triangle: Results from Belle and Babar



- Triangles in CKM
- B factories & experiments
- Update on measurements

$$|V_{td}|$$

$$|V_{cb}|$$

$$|V_{ub}|$$

- Conclusion & Summary



Introduction

Cabibbo-Kobayashi-Maskawa (CKM) matrix

{weak \leftrightarrow mass} eigenstates

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \mathcal{M} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$\begin{matrix} & \begin{matrix} d & s & b \end{matrix} \\ \begin{matrix} u \\ c \\ t \end{matrix} & \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \end{matrix}$$

to make
W-couplings
generation-conserving

$$g_F \times \begin{matrix} & \begin{matrix} d' & s' & b' \end{matrix} \\ \begin{matrix} u \\ c \\ t \end{matrix} & \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \end{matrix}$$

complex
preserves metric
" orthogonality } \equiv unitary

Unitarity conditions $V_{ji}^* V_{jk} = \delta_{ik}$ \rightarrow 4 free parameters

explicit parametrization (Wolfenstein):

$$\begin{pmatrix} 1 - \lambda^2/2 & \lambda & \lambda^3 A(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & \lambda^2 A \\ \lambda^3 A(1 - \rho - i\eta) & -\lambda^2 A & 1 \end{pmatrix}$$

irreducibly complex! \rightarrow CP violation

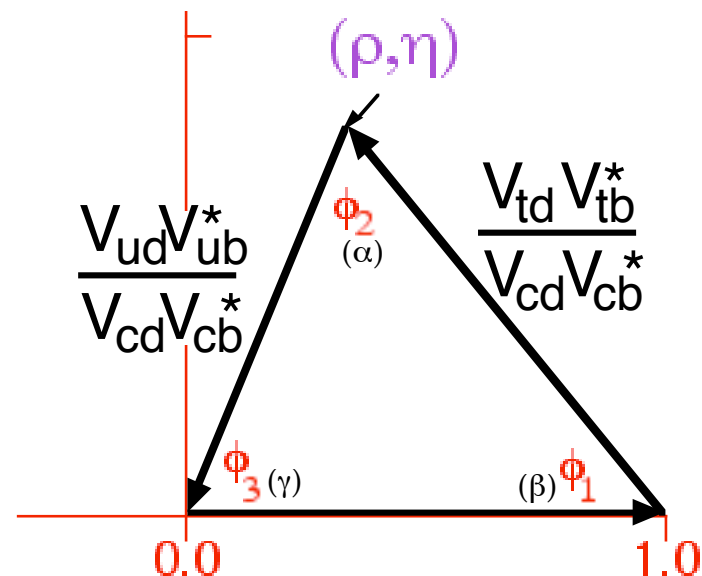
Unitarity conditions $V_{ji}^* V_{jk} = \delta_{ik}$

$$\{i=1, k=3\}: V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0$$

$$\Rightarrow \frac{V_{ub}^* V_{ud}}{V_{cb}^* V_{cd}} + 1 + \frac{V_{tb}^* V_{td}}{V_{cb}^* V_{cd}} = 0$$

\downarrow \downarrow
 $-(\rho+i\eta)$ $-(1-\rho-i\eta)$

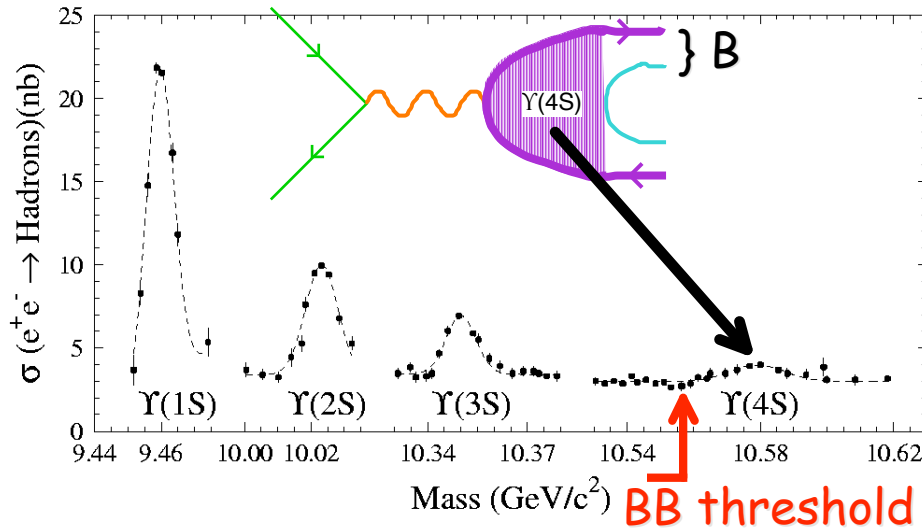
"unitarity triangle"



Objective of B-factories: test self-consistency of CKM

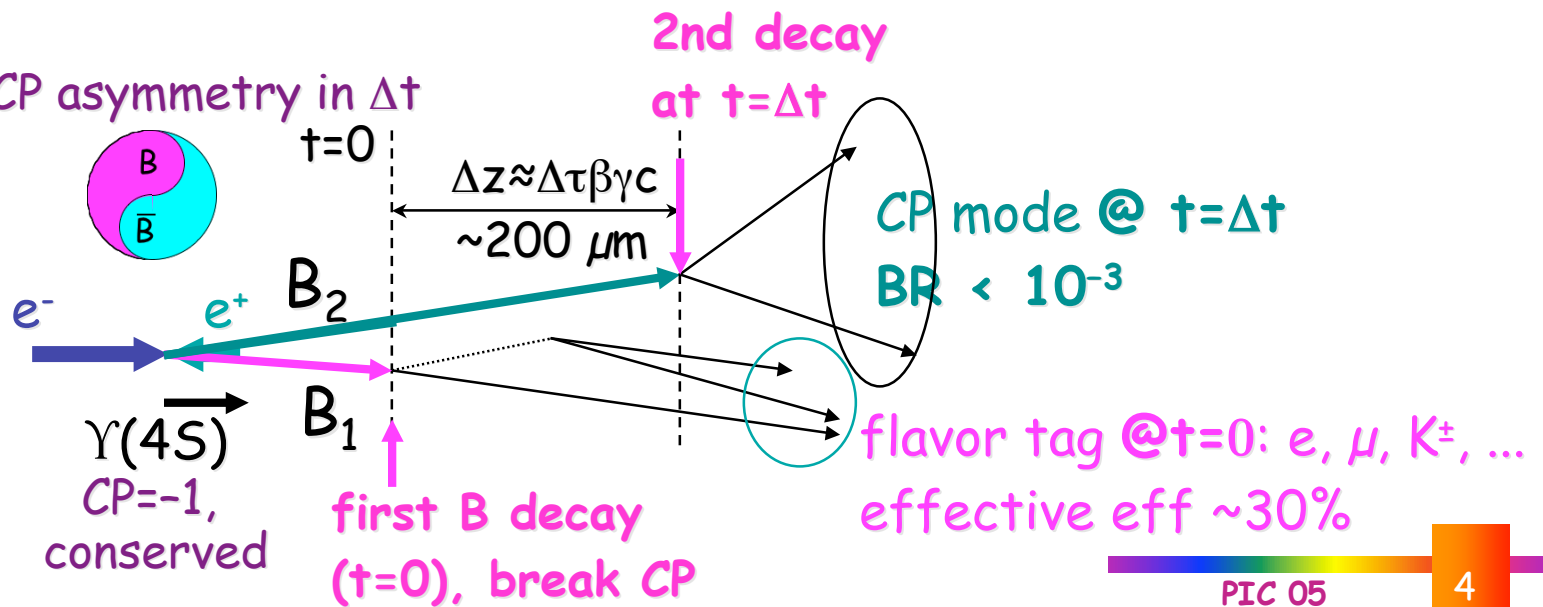
- Any 3 of {3 angles, 3 sides} fully constrains triangle
- Relevant magnitudes: $|V_{ub}|$, $|V_{cb}|$, $|V_{td}|$

B production: $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$

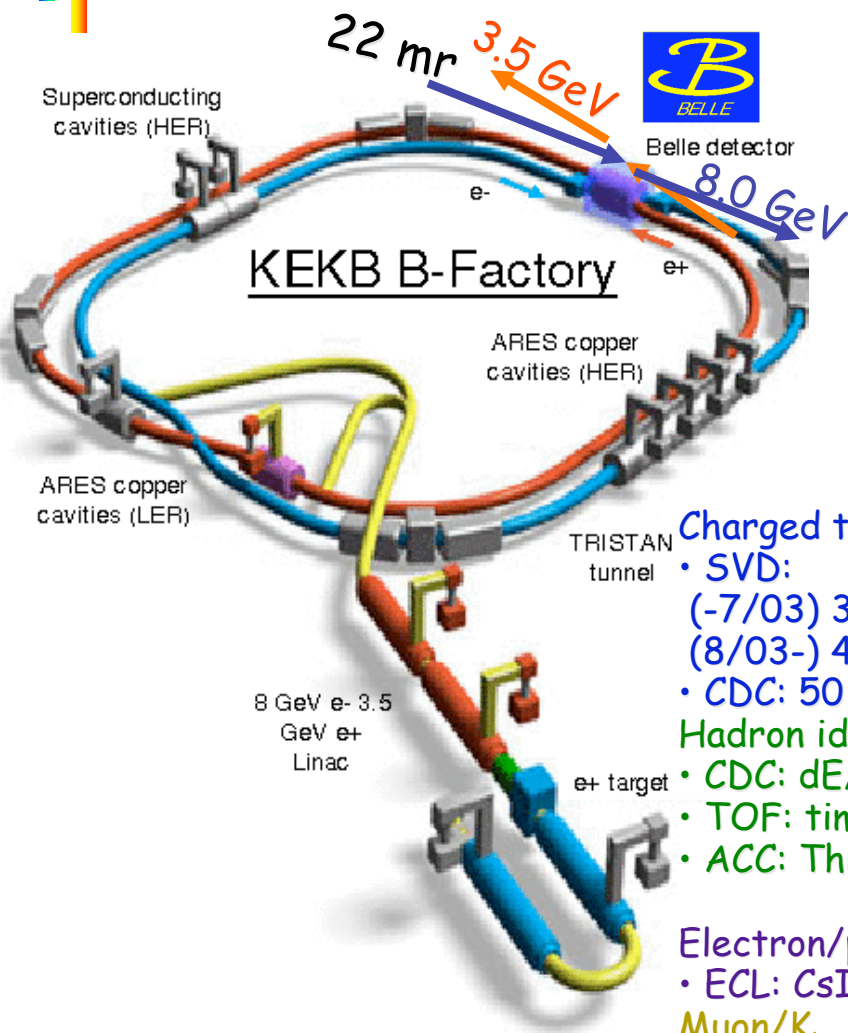


asymmetric energy $e^+e^- \rightarrow \Upsilon(4S)$
 (symmetric $\Upsilon(4S)$: CLEO 1979-2001)

B factories:
 designed for CP asymmetry in Δt



KEKB & Belle



- $L_{\max} = 1.588 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ (world record)
- Data (6/1999-6/2005)
- $\int L dt = 466 \text{ fb}^{-1} @ \{\Upsilon(4S) + \text{off}(\sim 10\%)\}$
- ($> 4.6 \times 10^8$ B events)

SVD1: 152M B pairs

SVD2: 123M+

Charged tracking/vertexing

- SVD:
 - (-7/03) 3-layer DSSD Si μ strip
 - (8/03-) 4-layer
- CDC: 50 layers (He-ethane)

Hadron identification

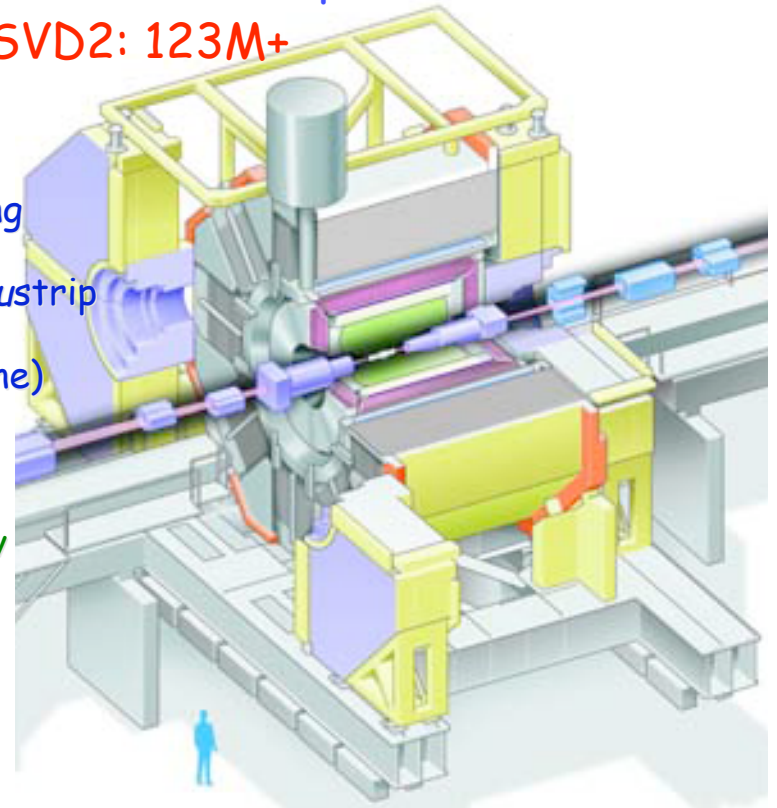
- CDC: dE/dx
- TOF: time-of-flight
- ACC: Threshold Cerenkov (aerogel)

Electron/photon

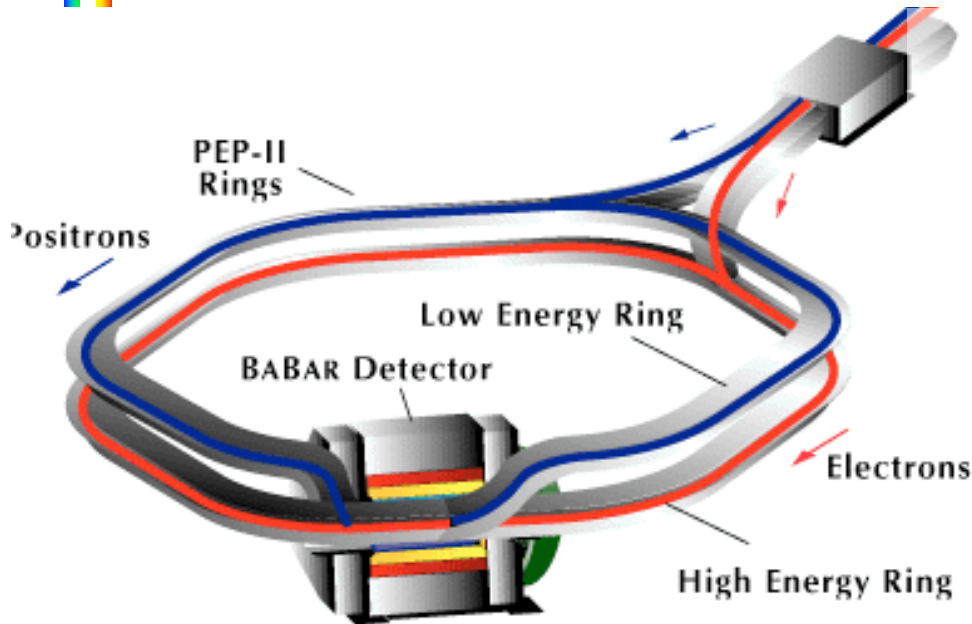
- ECL: CsI calorimeter

Muon/ K_L

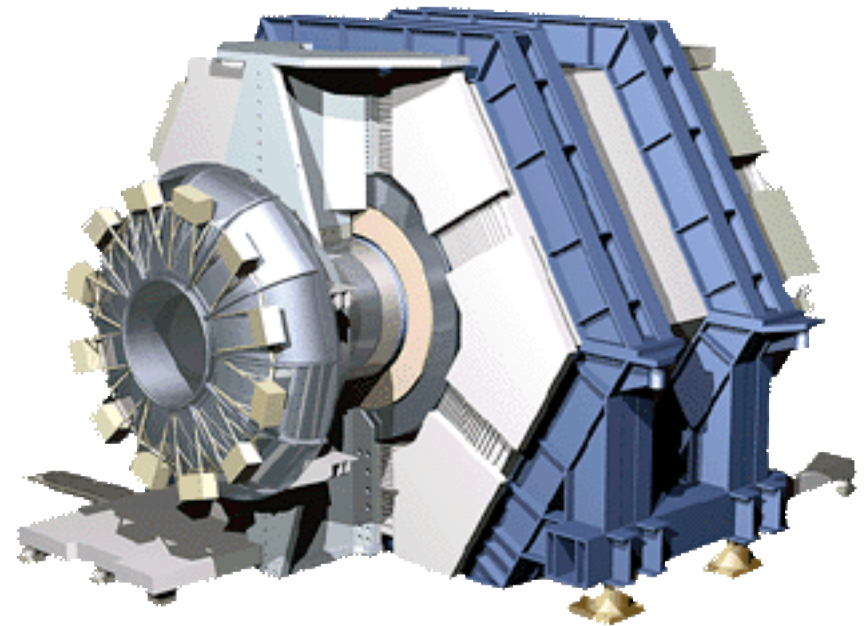
- KLM: Resistive plate counter/iron



PEP-II & Babar



- $L_{\max} = 9.2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
- Data (1999-4/2005)
- $\int L dt = 262 \text{ fb}^{-1} @ \{\Upsilon(4S) + \text{off}(\sim 10\%)\}$
- ($> 2.6 \times 10^8$ B events)



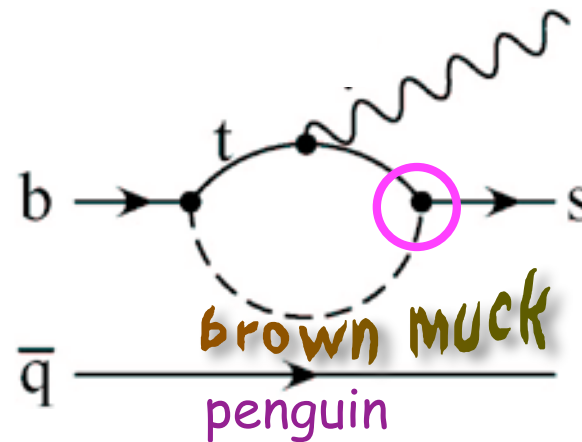
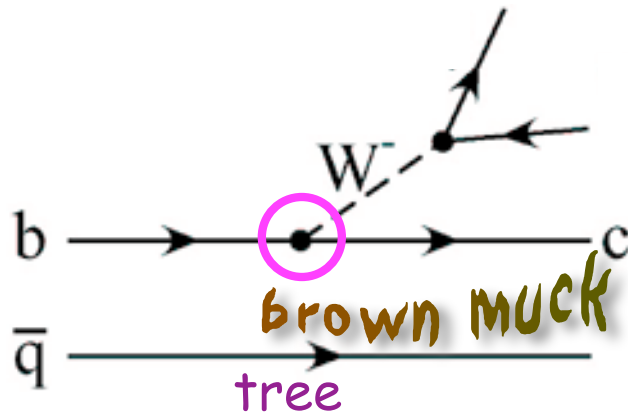
- Charged tracking/vertexing
 - 5-layer DSSD Si μ strip
 - 40 layers (He-isobutane)
- Hadron identification
 - tracker: dE/dx
 - DIRC imaging Cerenkov
- Electron/photon
 - CsI calorimeter
- Muon/ K_L
 - Instrumented flux return

~11 nations, 80 institutes, ~650 persons

Approach to measuring $|V_{ij}|$

Decay rates: $\Gamma \propto \sum_i^{\#states} |\mathcal{M}|^2$
 select mode(s):

- single dominant mechanism



- single unknown $|V_{ij}|$
- minimal hadronic uncertainty

unavoidable, limiting factor

continuing improvements

Experiment

Statistics → rare decays, restricted kinematic regions, detailed examination.

Theory

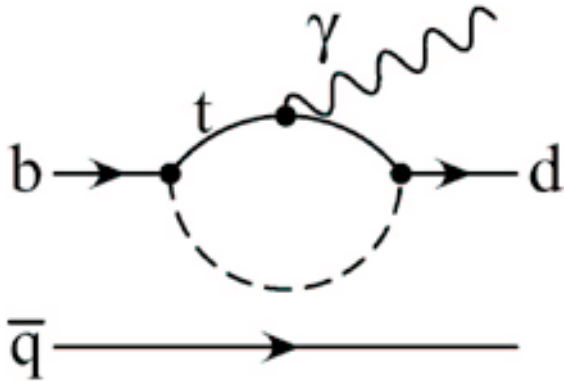
HQET, SCET, lattice, ...

ratios - compare decays, "same" proc.



$$|V_{td}|$$

b → dγ



$$\frac{\Gamma(b \rightarrow d\gamma)}{\Gamma(b \rightarrow s\gamma)} \propto \left| \frac{V_{td}}{V_{ts}} \right|^2$$

Ratio → reduced theory error ~10%

- inclusive measurement - preferred by theory
large (~30X) bg from b → sγ, similar kinematics
- exclusive B → {ρ/ω}γ - experimentally feasible
full reconstruction of decay

exploit

- exclusive pair production of B
- narrow resolution of collision energy

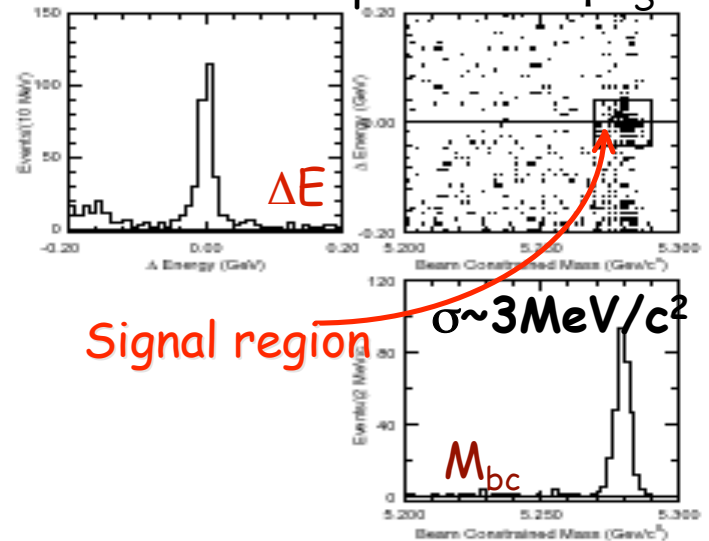
$$\Delta E = E_{\text{cand}}^* - E_{\text{beam}}^* = 0 \quad (E_{\text{beam}}^* = \sqrt{s}/2)$$

σ ~ 10-50 MeV, depends on mode

M_{bc} (Beam-constrained mass)

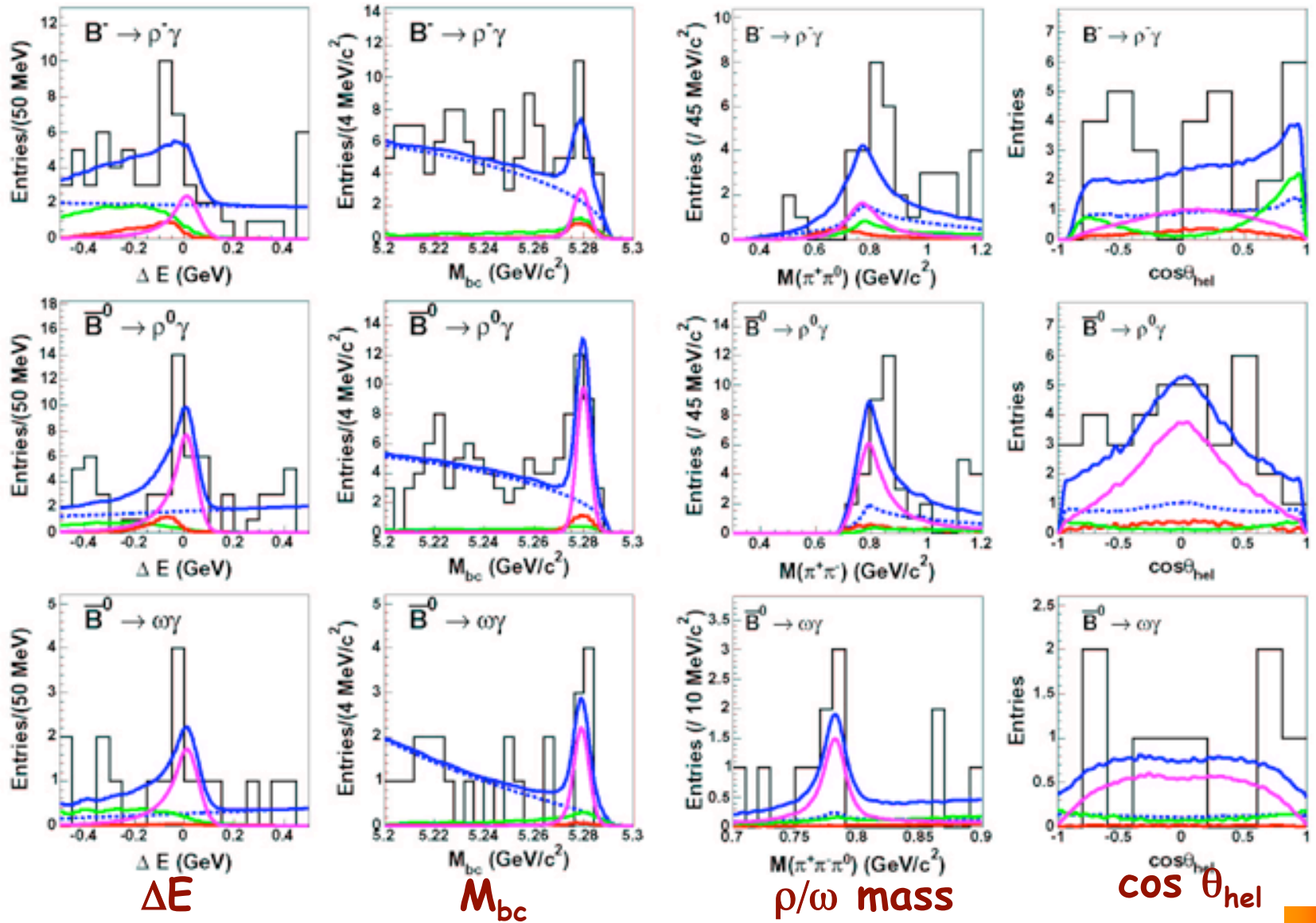
$$M_{bc} = (E_{\text{beam}}^{*2} - p_{\text{cand}}^{*2})^{1/2}$$

example: B → J/ψ K_S



Signal region

σ ~ 3 MeV/c²



b → d γ



386 M B evts (5.5σ)

Belle-CONF-0520 *preliminary*

(use isospin relations $\Gamma(B^- \rightarrow \rho^- \gamma) = 2\Gamma(B^0 \rightarrow \rho^0 \gamma) = 2\Gamma(B^0 \rightarrow \omega \gamma)$)

$$\mathcal{B}(B \rightarrow (\rho/\omega)\gamma) = (1.34_{-0.31}^{+0.34+0.14}) \times 10^{-6}$$

$\{= \mathcal{B}(B^- \rightarrow \rho^- \gamma)\}$

$$\frac{\mathcal{B}(B^- \rightarrow \rho^- \gamma)}{\mathcal{B}(B^- \rightarrow K^{*-} \gamma)} = 0.032 \pm 0.008_{-0.002}^{+0.003}$$

$$\left| \frac{V_{td}}{V_{ts}} \right| = (0.200_{-0.025}^{+0.026+0.038})$$



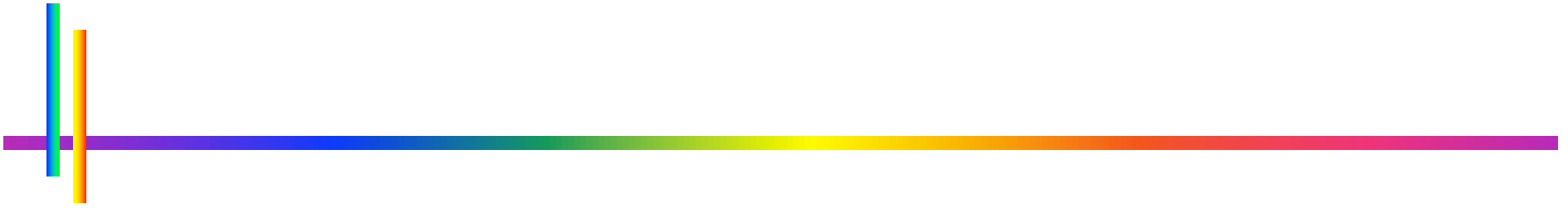
211 M B evts (2.1σ)

PRL 94, 011801 (2005)

$$\mathcal{B}(B^- \rightarrow \rho^- \gamma) < 1.2 \times 10^{-6} (90\% CL)$$

$$\frac{\mathcal{B}(B^- \rightarrow \rho^- \gamma)}{\mathcal{B}(B^- \rightarrow K^{*-} \gamma)} < 0.029 (90\% CL)$$

$$\left| \frac{V_{td}}{V_{ts}} \right| < 0.19 (90\% CL)$$

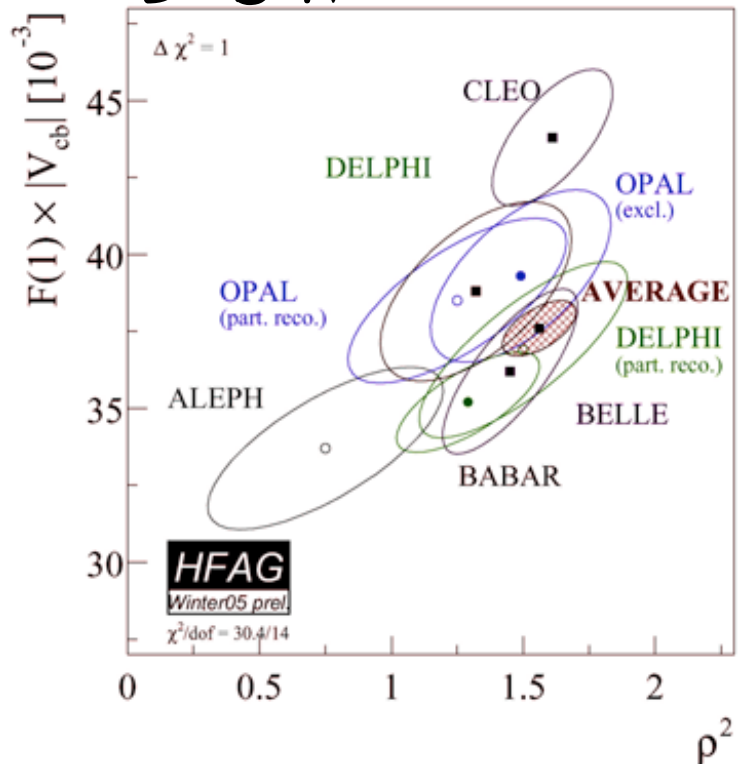


$$|V_{cb}|$$

Semileptonic $b \rightarrow c$ decays (no new results since Winter)

Exclusive modes (form factors)

$B \rightarrow D^* l \nu$

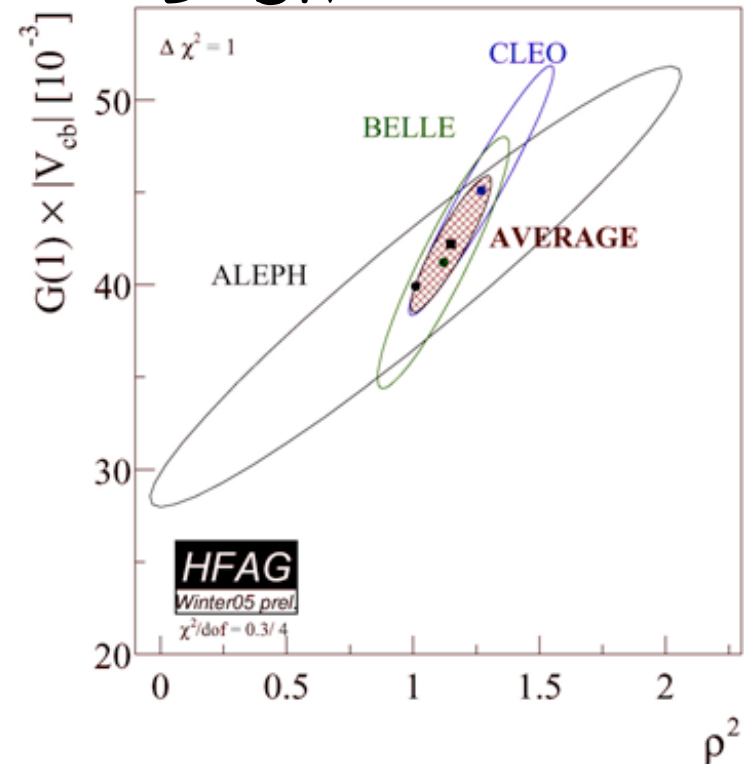


$$F(1)|V_{cb}| = (37.6 \pm 0.9) \times 10^{-3}$$

$$(F(1) = 0.91 \pm 0.04)$$

$$|V_{cb}| = (41.3 \pm 1.0 \pm 1.8) \times 10^{-3}$$

$B \rightarrow D l \nu$



$$G(1)|V_{cb}| = (42.2 \pm 3.7) \times 10^{-3}$$

$$(G(1) = 1.04 \pm 0.06)$$

$$|V_{cb}| = (40.6 \pm 3.6 \pm 1.3) \times 10^{-3}$$

Semileptonic $b \rightarrow c$ decays



hep-ex/0404017

Inclusive - opposite fully reconstructed B

- moments of E_l , M_X distributions
 - fit for params in "kinetic mass" scheme (Gambino&Uraltsev hep-ph/0401063)
- > $|V_{cb}| = (41.4 \pm 0.4 \pm 0.4 \pm 0.6) \times 10^{-3}$



hep-ex/0408139 *preliminary*

- moments of E_l , M_X distributions (140 fb^{-1})
- update in progress

Bauer et al, PRD70, 094017(2004) (hep-ph/0408002)

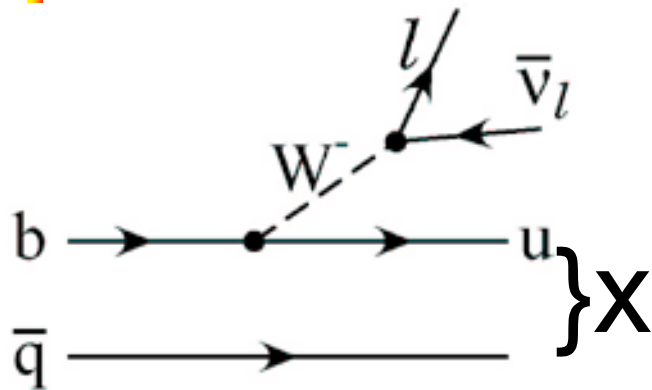
Global fit analysis: moments in the "1S" scheme \rightarrow PRL 82, 277 (1999);
PRD 59, 074017 (1999);
Using data from BaBar, Belle, CDF, CLEO & Delphi PRD 60, 114027 (1999)

$$|V_{cb}| = (41.4 \pm 0.6 \pm 0.1(\tau_B)) \times 10^{-3}$$



$|V_{ub}|$

Inclusive semileptonic $b \rightarrow u$ decays



Experimental methods

- inclusive lepton spectrum \rightarrow "endpoint"
- lepton + semi-inclusive hadronic
- lepton + "neutrino"
- w/wo (full reconstruction) tagging

Issues

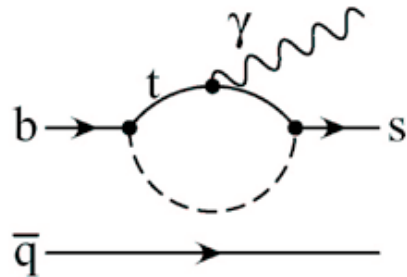
- huge bg from $b \rightarrow c$
- uncertainties on X_u, X_c
- Relevant kinematic variables
 - Theory: 4-mom., polarization of W
 - uncertainties vary w. region
 - {OPE, HQET, SF, ...}
 - Expt: lepton mom., missing E&p, M_X
 - (not 1-to-1)

Recent improvements

- "shape function" - relate X :
 $b \rightarrow ul\nu, b \rightarrow s\gamma, b \rightarrow cl\nu$
- Variables balance theoretical & exp'tal relevance: $q^2, M_X, P_+ = E_X - |P_X|$
- direct $|V_{ub}|$ from partial rate
Lange, Neubert, Paz, hep-ph/0504071

HQET parameters for V_{ub} : spectrum of $b \rightarrow s \gamma$

HQET parameters from fit to E_γ spectrum from $b \rightarrow s \gamma$

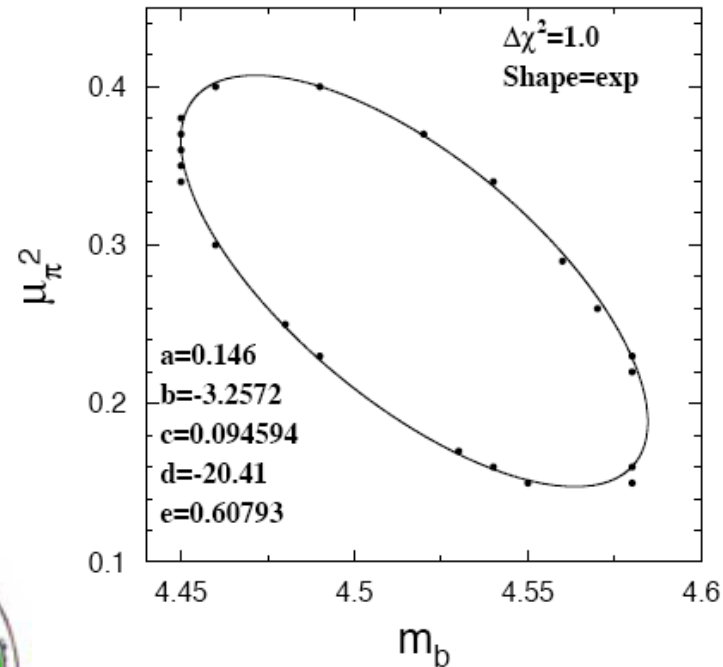
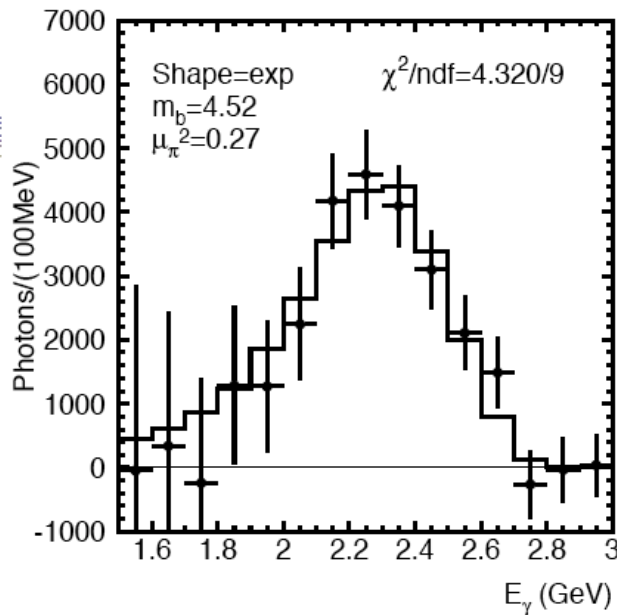


shape: Lange, Paz & Neubert
 hep-ph/0504071 (LNP)

Belle fit (hep-ex/0506057)

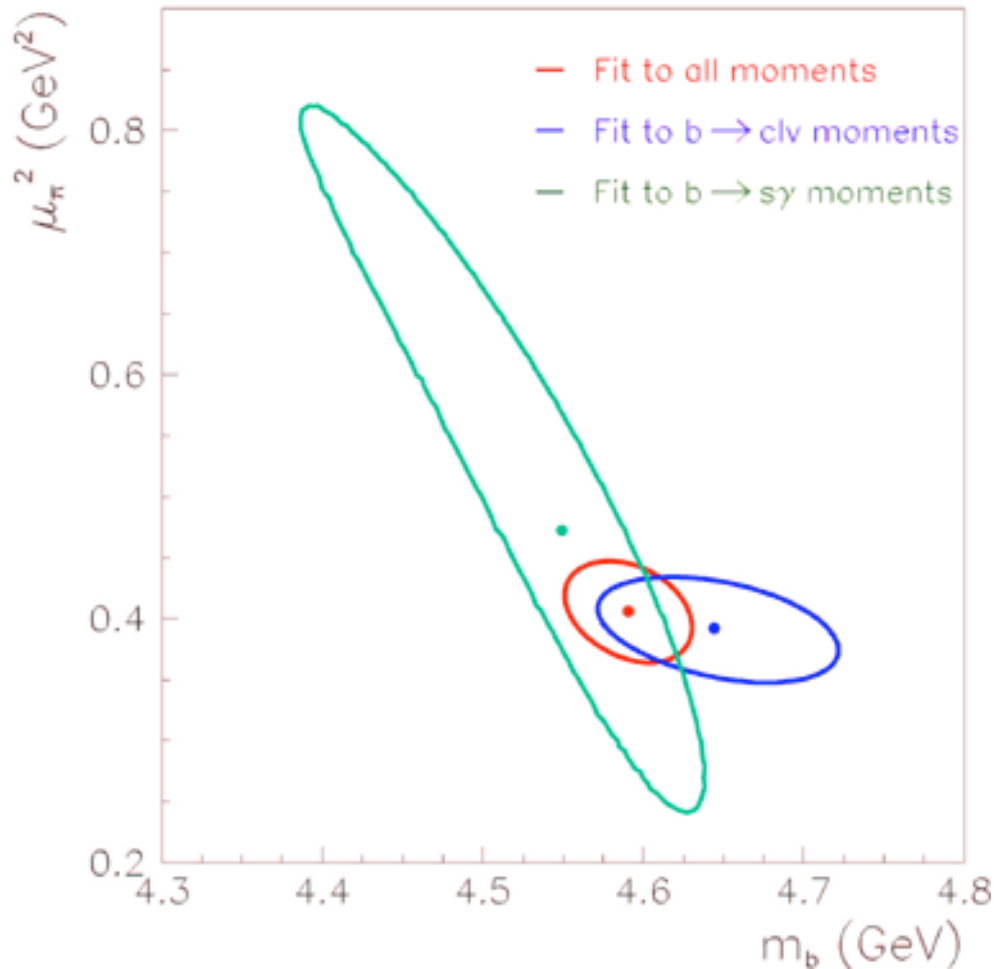
$$m_b(\text{SF}) = 4.52 \text{ GeV}/c^2;$$

$$\mu_\pi^2(\text{SF}) = 0.27 \text{ GeV}^2/c^2$$



Babar: hep-ex/0506043

HQET parameters for V_{ub} : HFAG



Fit for moments
to data: $b \rightarrow s\gamma$ and $b \rightarrow c l \nu$
Kinetic Scheme
(Gambino&Uraltsev hep-ph/0401063)

Translated to
Shape Function Scheme
(Neubert Phys.Lett.B612:13-20,2005):
 $m_b(\text{SF}) = (4.60 \pm 0.04) \text{ GeV}/c^2$;
 $M_\pi^2(\text{SF}) = (0.20 \pm 0.04) \text{ GeV}^2/c^2$

<http://www.slac.stanford.edu/xorg/hfag/semi/lp05/globalFit.html>

Lepton momentum endpoint

$|V_{ub}|$: theory uncertainties

- exclusive modes
- inclusive: shape function

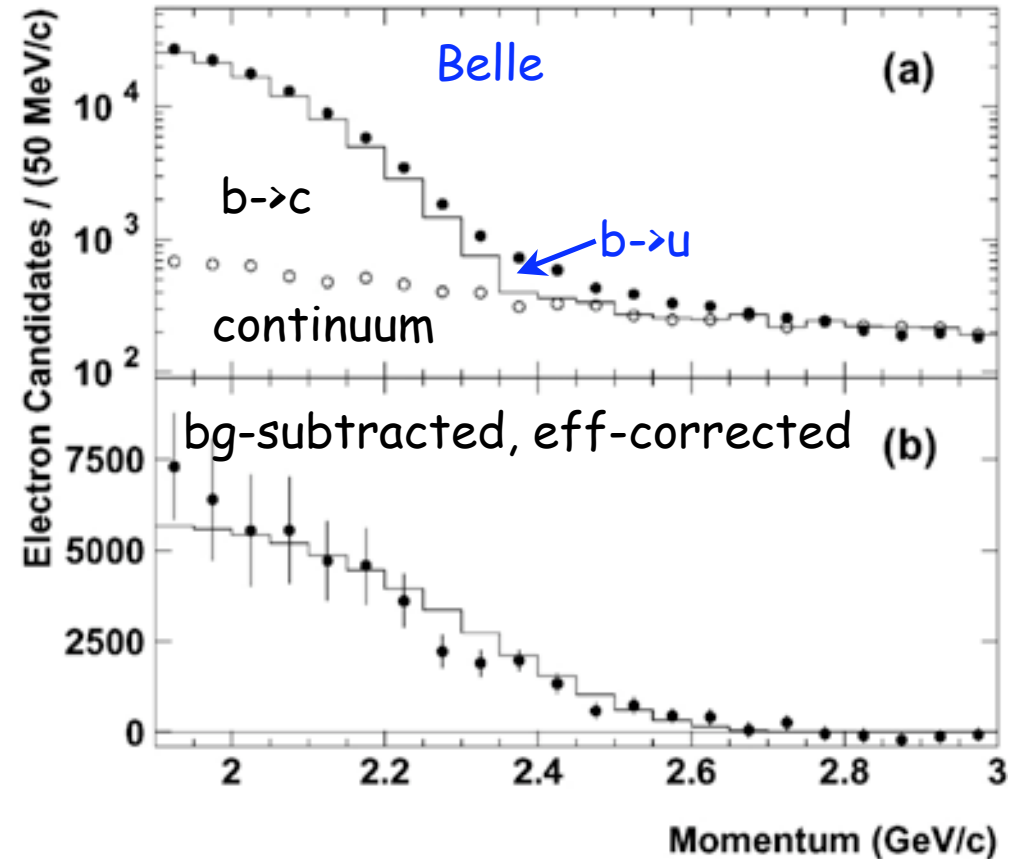


- cuts maximize q^2 acceptance
- endpt region 1.9-2.6 GeV/c to minimize err (expt+th)
- shape function: fit to $b \rightarrow s$
- $\Delta B \rightarrow |V_{ub}|$ via LNP



- endpt region 2.0-2.6 GeV/c
- shape function: $b \rightarrow s$ from CLEO (also w Belle fit)
- $\Delta B \rightarrow |V_{ub}|$ via

Uraltsev Int. J. Mod. Phys. A14, 4641 (1999); Hoang, Ligeti, Manhar PRD 59, 074017 (1999)



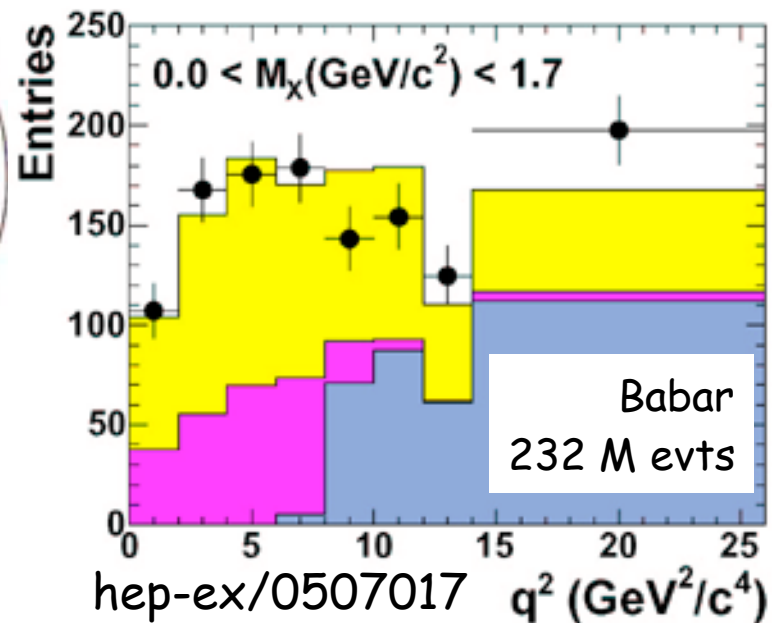
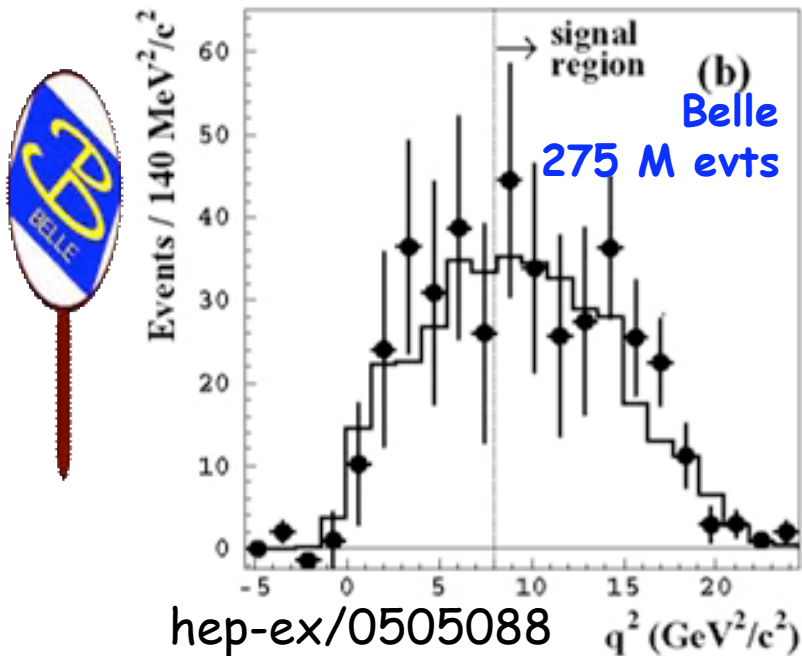
Exploring M_X, q^2, P_+

Full reconstruction tag + lepton + M_X

- high signal purity \rightarrow higher p_1 acceptance
- explore phase space \rightarrow reduce sys errors
- cuts to reduce theory uncertainty

($q^2 > 8.0 \text{ GeV}^2/c^2, M_X < 1.7 \text{ GeV}/c^2$; Bauer, Ligeti & Luke, Phys.Rev.D64:113004 (2001))

- direct $\Delta B \rightarrow |V_{ub}|$ (LNP)



Exploring M_X, q^2, P_+

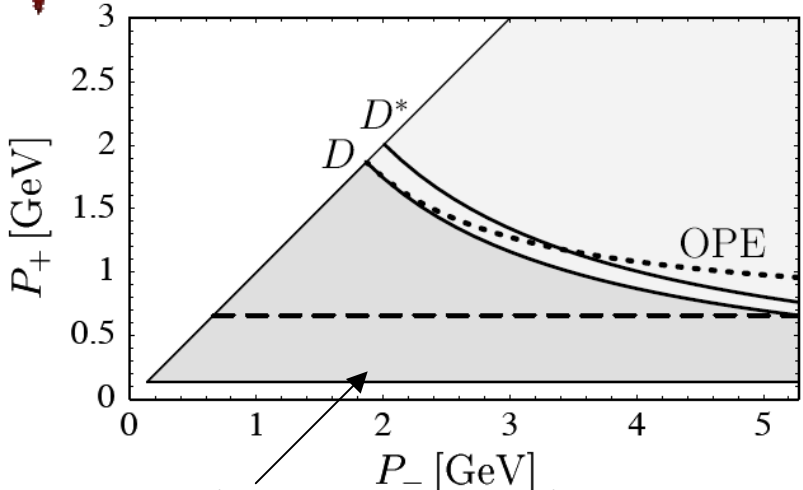


hep-ex/0505088

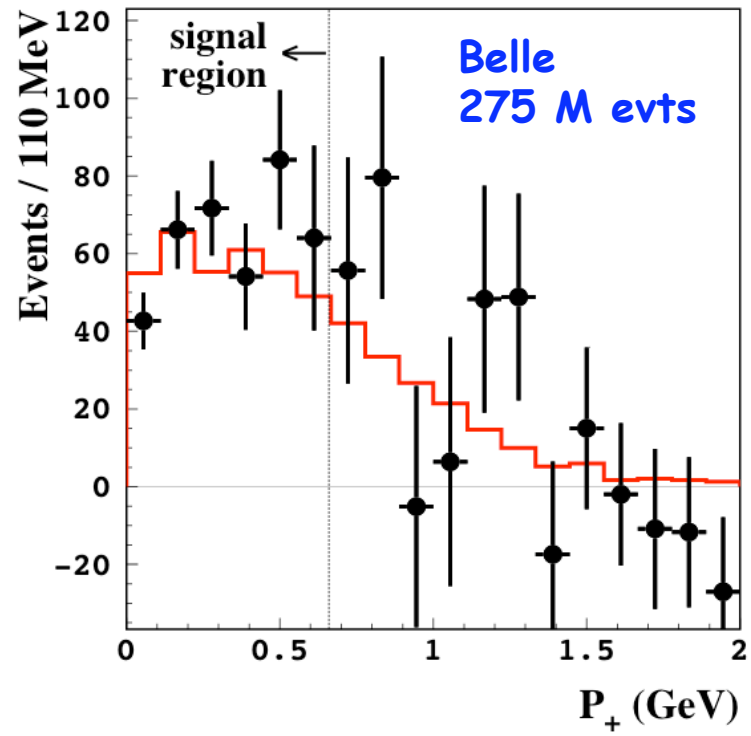
- measure distribution in P_+ :
higher yield w low background
(PRL 93, 221801 (2004))
- direct $\Delta B \rightarrow |V_{ub}|$ (LNP)

$$P_+ = E_X - P_X$$

$$P_- = E_X + P_X$$



Avoid $b \rightarrow c$ background
Min. theory uncertainty
 $P_+ < 0.66$ GeV



Exploring M_X, q^2, P_+

hep-ex/0506036

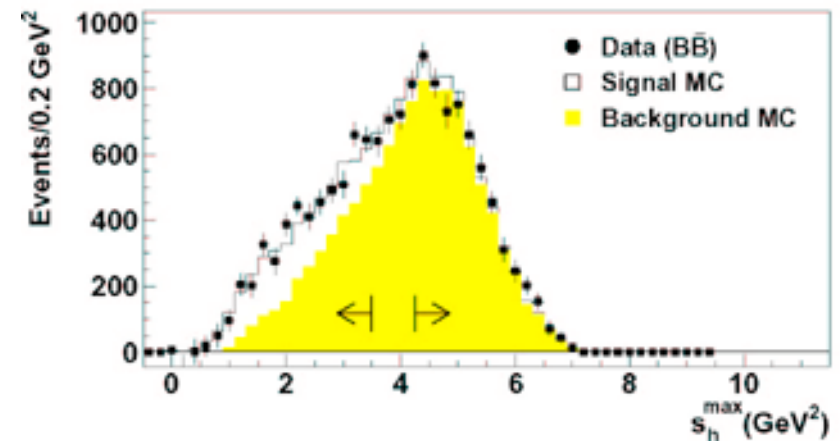
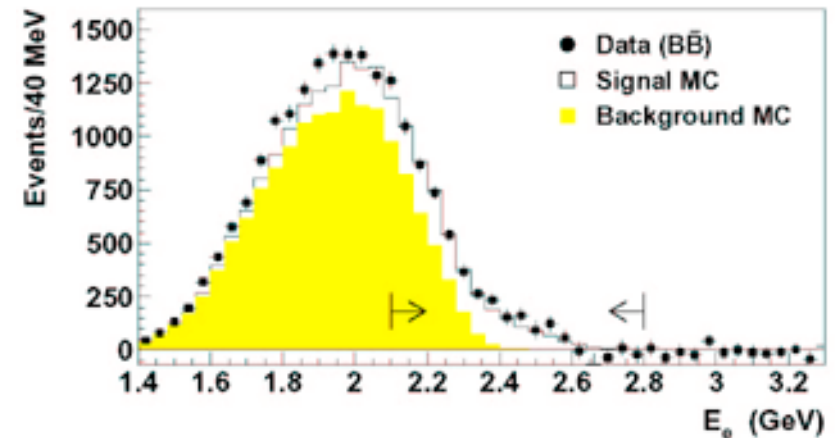
endpoint $e^\pm + \nu$ reconstruction

- ΔB for cuts in rest frame of B

$$E_e > 2.0 \text{ GeV}$$

$$s_h^{\max} < 3.5 \text{ GeV}^2 \text{ (}\{\text{max hadronic recoil mass}\}^2\text{)}$$

- direct $\Delta B \rightarrow |V_{ub}|$ via LNP



Summary of $|V_{ub}|$ measurements

($|V_{ub}|$ as reported; errors: $\pm(\text{experimental}) \pm(\text{theory})$)

Belle	reference	$\Delta\mathcal{B} \times 10^4$	$ V_{ub} \times 10^3$
Endpoint (29M $B\bar{B}$)	hep-ex/0504046		
$1.9 < p_\ell < 2.6 \text{ GeV}/c$		$8.47 \pm 0.37 \pm 1.53$	$5.08 \pm 0.47 \pm 0.49$
Full reconstruction tag ($p_\ell^* > 1 \text{ GeV}/c$)	hep-ex/0505088		
$M_X < 1.7 \text{ GeV}/c^2, q^2 > 8 \text{ GeV}^2/c^2$		$8.41 \pm 1.14 \pm 0.69$	$4.93 \pm 0.33 \pm 0.57$
$M_X < 1.7 \text{ GeV}/c^2$		$12.4 \pm 1.5 \pm 0.8$	$4.35 \pm 0.25 \pm 0.46$
$P_+ < 0.66 \text{ GeV}/c$		$11.0 \pm 1.5 \pm 1.2$	$4.56 \pm 0.30 \pm 0.59$
Babar			
Endpoint (88M $B\bar{B}$)	hep-ex/0408075		
$2.0 < p_\ell^* < 2.6 \text{ GeV}/c$		$4.80 \pm 0.29 \pm 0.53$	$3.94 \pm 0.25 \pm 0.42$
E_e, ν reconstruction (88M $B\bar{B}$)	hep-ex/0506036		
$\tilde{E}_e > 2.0 \text{ GeV}, \tilde{s}_h^{max} < 3.5 \text{ GeV}^2$		$3.54 \pm 0.33 \pm 0.34$	$3.95 \pm 0.26^{+0.63}_{-0.49}$
Full reconstruction tag ($p_\ell^* > 1 \text{ GeV}/c$)	hep-ex/0507017		
$M_X < 1.7 \text{ GeV}/c^2, q^2 > 8 \text{ GeV}^2/c^2$		$8.7 \pm 1.3 \pm 0.1$	$4.65 \pm 0.34 \pm 0.49$

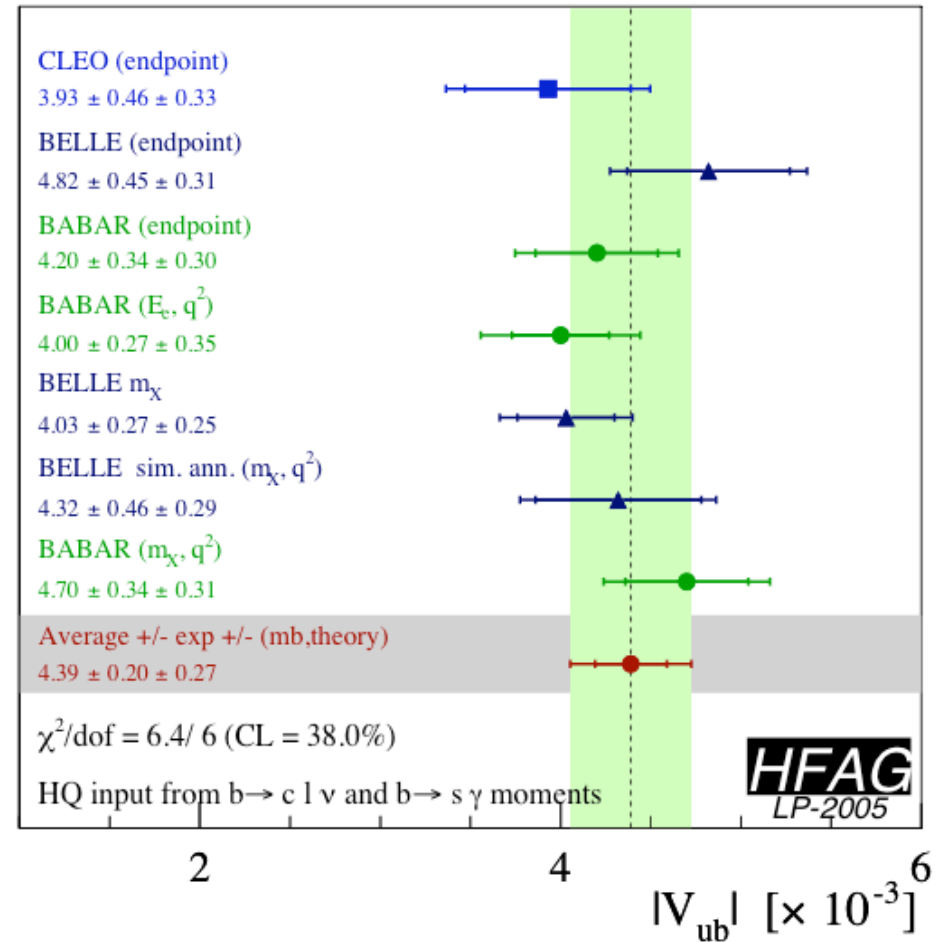
&more.

Warning! Can't compare $|V_{ub}|$ directly - different methods & inputs

Roundup of $|V_{ub}|$ via inclusive semileptonic: HFAG

Many results, hard to compare

- shape function, HQ parameter fits Belle/Babar/CLEO data
- parametrizations: SF, kinetic schemes
- fits included: $b \rightarrow c l \nu$ and/or $b \rightarrow s$
- kinematic cuts vary
- $\Delta B \rightarrow |V_{ub}|$ new results: dust may not have settled
- need unified presentation --> HFAG
- <http://www.slac.stanford.edu/xorg/hfag>
- * Common theoretical input
- HQET parameters from global fit to moments of $b \rightarrow c l \nu$ and/or $b \rightarrow s \gamma$ (3 combos)
- BLNP hep-ph/0504071
- * Correlated $b \rightarrow X l \nu$ modeling errors



preliminary

$$|V_{ub}| = (4.39 \pm 0.20(\text{exp}) \pm 0.27(m_b, \text{theory})) \times 10^{-3} \quad [b \rightarrow c l \nu \text{ and } b \rightarrow s \gamma]$$

Roundup ... at the moment,

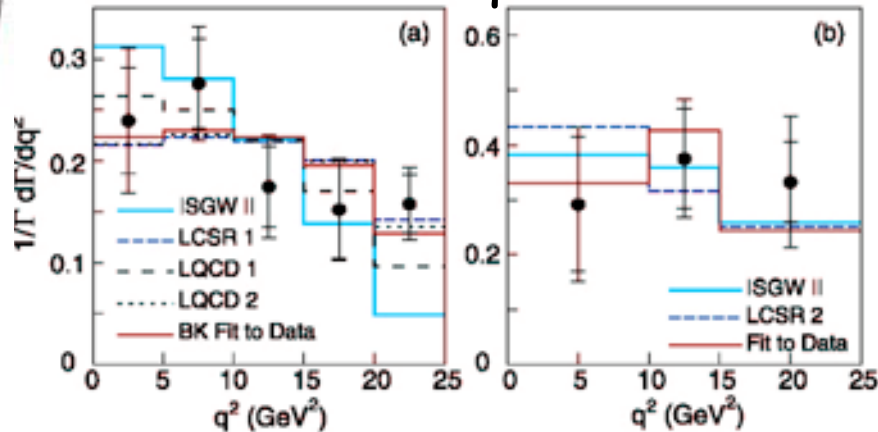
... still under discussion ...



Exclusive semileptonic



$\pi/\rho|v; \nu$ reconstruction) hep-ex/0507003
in bins of q^2



LCSR1: Ball&Zwicky, PRD71, 014015 (2005)
LCSR2: Ball&Zwicky, PRD71, 014029 (2005)
LQCD1: Shigemitsu&al, hep-lat/0408019
LQCD2: Okamoto&al, hep-lat/0409116
ISGWII: Scora&Isgur, PRD52, 2783 (1995)

$\Delta B \rightarrow |V_{ub}|$:

Light-cone sum rules (low q^2 only)

Unquenched lattice QCD (high q^2)



preliminary
hep-ex/0408145

	q^2 Range (GeV ²)	$\Delta\zeta$ (ps ⁻¹)	$ V_{ub} $ (10 ⁻³)
π FF			
LCSR1	0-15	5.1±1.3	3.27 ± 0.16 ± 0.19 ± 0.10 ^{+0.53} _{-0.36}
LQCD1	15-25	1.5±0.4	4.92 ± 0.25 ± 0.29 ± 0.15 ^{+0.76} _{-0.52}
LQCD2	15-25	2.0±0.5	4.16 ± 0.22 ± 0.24 ± 0.12 ^{+0.72} _{-0.47}
LCSR1	0-25	7.7±2.3	3.40 ± 0.13 ± 0.20 ± 0.10 ^{+0.67} _{-0.42}
LQCD1	0-25	5.7±1.7	4.00 ± 0.14 ± 0.23 ± 0.12 ^{+0.78} _{-0.49}
LQCD2	0-25	6.1±2.1	3.82 ± 0.14 ± 0.22 ± 0.11 ^{+0.88} _{-0.52}
ρ FF			
LCSR2	0-15	12.7	2.82 ± 0.18 ± 0.30 ± 0.18
ISGW II	0-25	14.2	2.91 ± 0.12 ± 0.33 ± 0.19
LCSR2	0-25	17.2	2.85 ± 0.14 ± 0.32 ± 0.19

FF	q^2	$ V_{ub} $ (10 ⁻³)
LQCD1	> 16 GeV ²	4.73 ± 0.85 ± 0.27 ^{+0.74} _{-0.50}
LQCD2	> 16 GeV ²	3.87 ± 0.70 ± 0.22 ^{+0.85} _{-0.51}

Exclusive semileptonic



Tag by exclusive semileptonic $B \rightarrow D^{(*)} l \nu$;
require kinematic consistency

$\pi^+ l \nu$; hep-ex/0506064 (211 fb⁻¹)

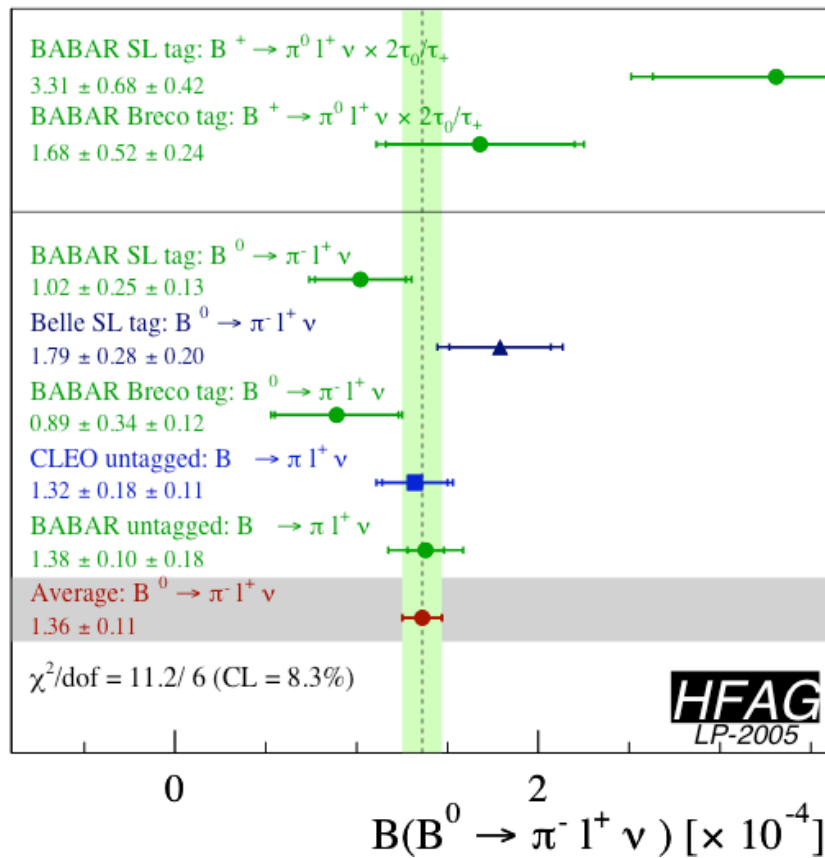
bins of q^2

preliminary

FF calculation	q^2 range	$\Delta\zeta$ (ps ⁻¹)	$ V_{ub} $ (10 ⁻³)
Ball-Zwicky [2]	$< 16 \text{ GeV}^2$	5.44 ± 1.43	$3.1 \pm 0.4_{\text{stat.}} \pm 0.2_{\text{syst.}}^{+0.5}_{-0.3\text{FF}}$
HPQCD [3]	$> 16 \text{ GeV}^2$	1.29 ± 0.32	$3.3 \pm 1.1_{\text{stat.}} \pm 0.5_{\text{syst.}}^{+0.5}_{-0.3\text{FF}}$
FNAL [4]	$> 16 \text{ GeV}^2$	1.83 ± 0.50	$2.7 \pm 0.9_{\text{stat.}} \pm 0.4_{\text{syst.}}^{+0.5}_{-0.3\text{FF}}$
Ball-Zwicky [2]	full	7.74 ± 2.32	$2.9 \pm 0.4_{\text{stat.}} \pm 0.2_{\text{syst.}}^{+0.6}_{-0.4\text{FF}}$
HPQCD [3]	full	5.70 ± 1.71	$3.4 \pm 0.4_{\text{stat.}} \pm 0.2_{\text{syst.}}^{+0.7}_{-0.4\text{FF}}$
FNAL [4]	full	6.24 ± 2.12	$3.3 \pm 0.4_{\text{stat.}} \pm 0.2_{\text{syst.}}^{+0.8}_{-0.4\text{FF}}$

$\pi^0 l \nu$; hep-ex/0506065 (81 fb⁻¹)

Roundup of $|V_{ub}|$ via exclusive semileptonic: HFAG



preliminary

From avg ΔB ($q^2 > 16 \text{ GeV}^2$)

LQCD2 ->

$$|V_{ub}| = (3.75 \pm 0.27 + 0.64 - 0.42) \times 10^{-3}$$

LQCD1 ->

$$|V_{ub}| = (4.45 \pm 0.32 + 0.69 - 0.47) \times 10^{-3}$$

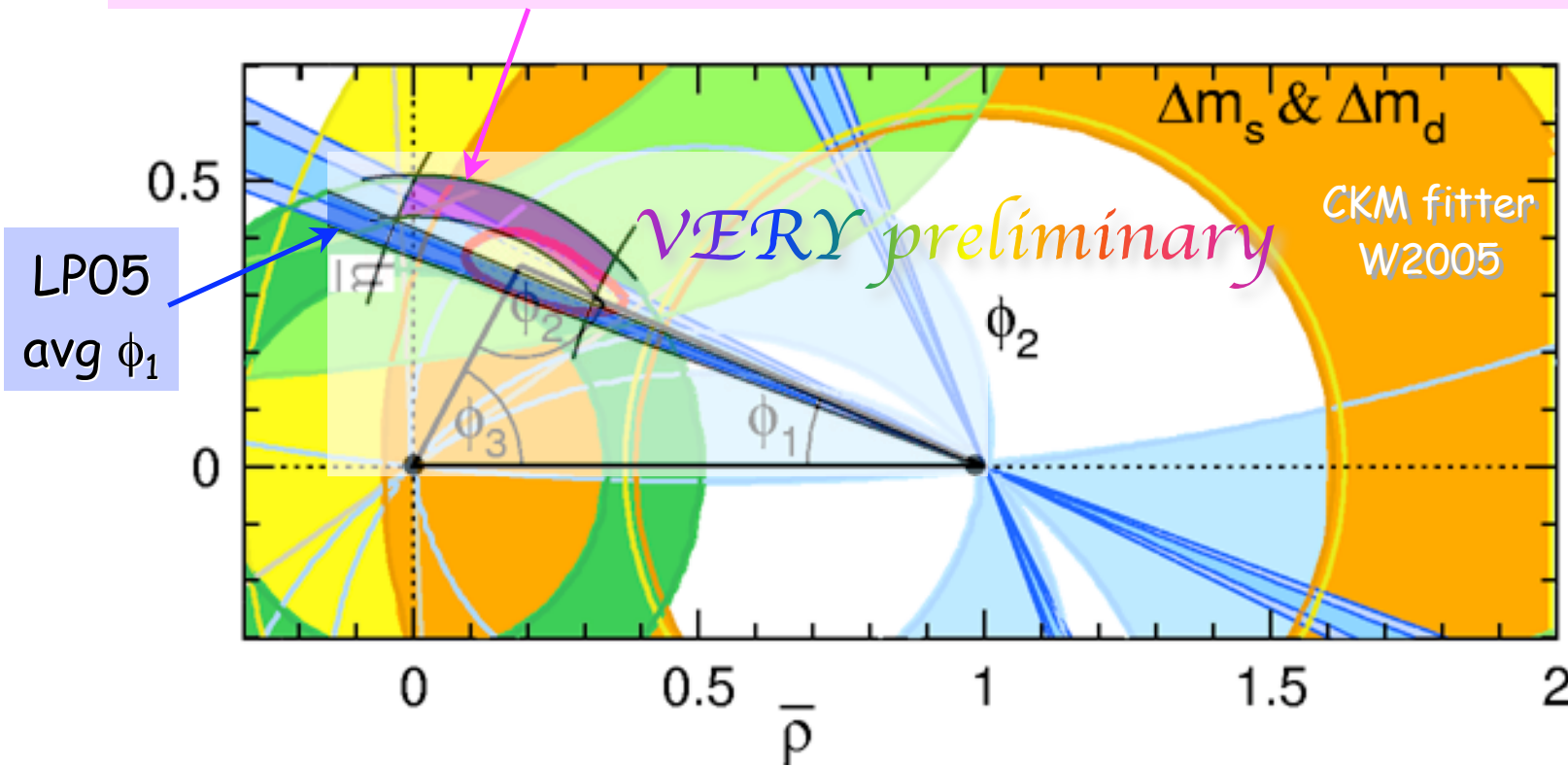
1st err: experimental

2nd err: normalization uncertainty in form factor calculation.

CKM status

$$|V_{td}/V_{ts}| = \lambda|1-\rho-\eta| \quad \Rightarrow \quad |1-\rho-\eta| = 0.91^{+0.21}_{-0.17} \quad [b \rightarrow d\gamma]$$

$$|V_{ub}/V_{cb}| = \lambda|\rho-\eta| \quad \Rightarrow \quad |\rho-\eta| = 0.48 \pm 0.04 \quad [b \rightarrow ul\nu \text{ inclusive}]$$



Conclude: $|V_{ij}|$ can play a major role in (over)constraining CKM

Summary

B Factories 1999-2005:

- Total $> 7.3 \times 10^8$ B pairs
- CKM Unitarity Triangle -
precision measurement of sides \rightarrow overconstraint
- $|V_{td}|$ - first evidence for $b \rightarrow d$ $\rightarrow \pm 13\%$
- $|V_{cb}|$ - continued progress, p_l/M_X moments $\rightarrow < \pm 2\%$
- $|V_{ub}|$ - many semileptonic measurements,
progress on theory (inclusive and exclusive modes)
higher precision $< \pm 10\%$ but accuracy?(under discussion)

Next

- complete unfinished LP05 abstracts \rightarrow EPS
- continue interaction w theorists
- more data
- \rightarrow improving precision on sides as well as angles;
CKM challenge is heating up - stay tuned!