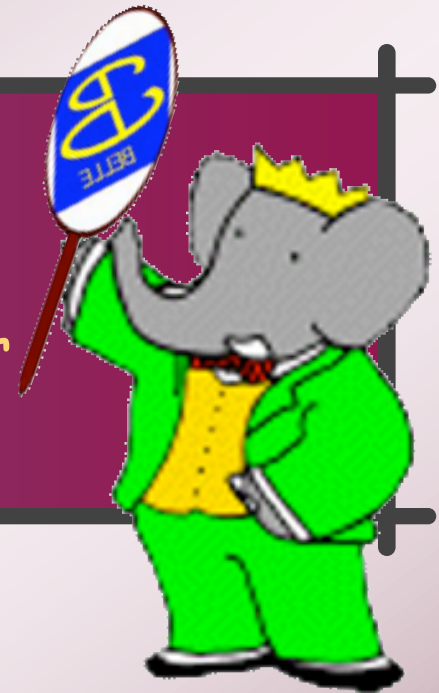


CKM Reflections: Results from Belle and Babar



- CP asymmetry in CKM
- B factories & experiments
- Measurements of $\sin 2\phi_1$
- Progress on $\sin 2\phi_2$
- Progress on $\sin 2\phi_3$
- Other CKM
- Summary

CKM and CP Asymmetry

Complex coupling constant is CP-violating

$$CP\{f \xrightarrow{g} f'\} = \bar{f}' \xleftarrow{g} \bar{f} \neq \bar{f}' \xleftarrow{g^*} \bar{f} \text{ (hermitian conjugate)}$$

BUT to observe CP asym, need 2+ interfering amplitudes {T,P}:

$$T=gA, P=g'A' \rightarrow |gA+g'A'| \xrightarrow{CP} |gA^*+g'A'^*|$$

Equal only if relative phase of $g, g'=0$

Cabibbo-Kobayashi-Maskawa (CKM) matrix

{weak \leftrightarrow mass} eigenstates

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \mathcal{M} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

so that
W-couplings are
generation-conserving

$$g_F \times \begin{matrix} u \\ c \\ t \end{matrix} \begin{pmatrix} d' & s' & b' \\ \mathbf{1} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{1} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{1} \end{pmatrix}$$

$$\begin{matrix} u \\ c \\ t \end{matrix} \begin{pmatrix} d & s & b \\ V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

complex
preserves metric
" orthogonality

\equiv unitary

+ in 3-d,
irreducibly
complex

3-generation CKM

Unitarity conditions -> 4 free parameters

$$V_{ji}^* V_{jk} = \delta_{ik}$$

$$\{i=1, k=3\}: V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0$$

$$\Rightarrow \frac{V_{ub}^* V_{ud}}{V_{cb}^* V_{cd}} + 1 + \frac{V_{tb}^* V_{td}}{V_{cb}^* V_{cd}} = 0$$

$$-(\rho + i\eta)$$

$$-(1 - \rho - i\eta)$$

explicit parametrization (Wolfenstein):

$$\begin{pmatrix} 1 - \lambda^2/2 & \lambda & \lambda^3 A(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & \lambda^2 A \\ \lambda^3 A(1 - \rho - i\eta) & -\lambda^2 A & 1 \end{pmatrix}$$

irreducibly complex!

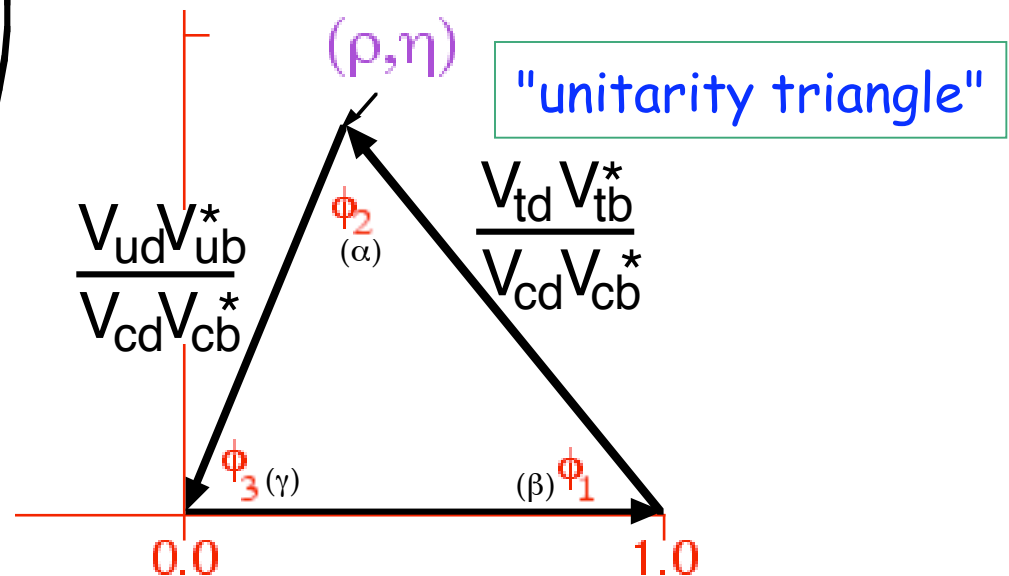
from decay rates,

$$\lambda = 0.220 \pm 0.002$$

$$A = 0.81 \pm 0.08$$

$$|\rho - i\eta| = 0.36 \pm 0.09$$

$$|1 - \rho - i\eta| = 0.79 \pm 0.19$$

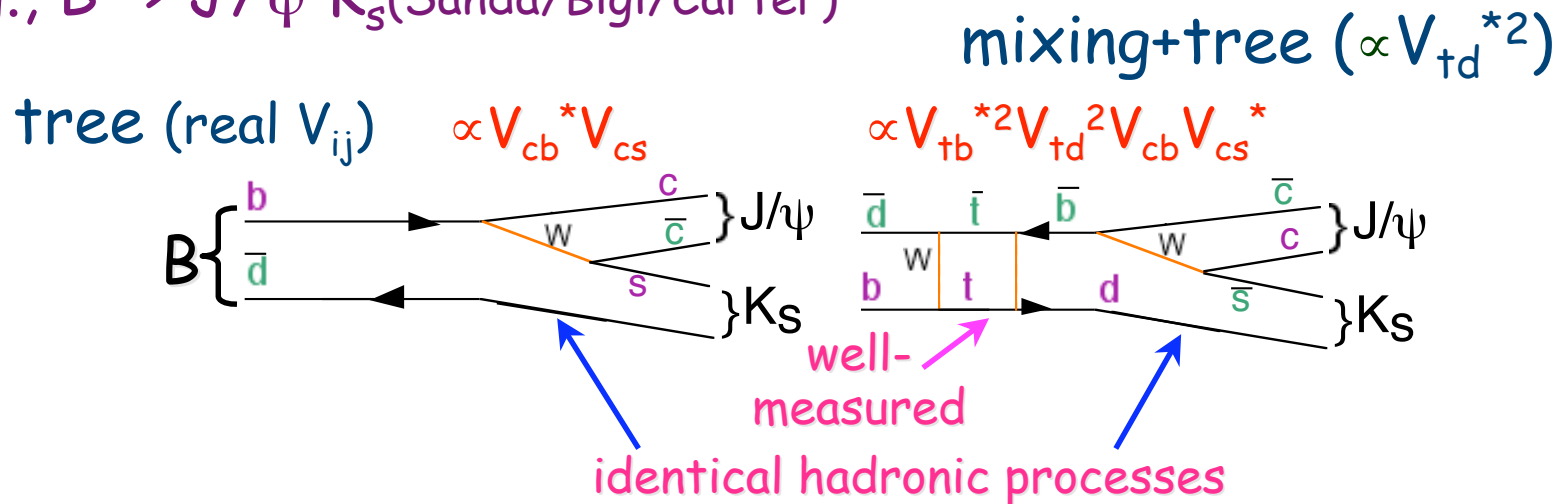


B-factories: measure angles, test self-consistency of CKM

Observable CP asymmetries

-> to observe, need process w. all 3 generations (<- B decays),
interference between ≥ 2 processes

e.g., $B \rightarrow J/\psi K_S$ (Sanda/Bigi/Carter)



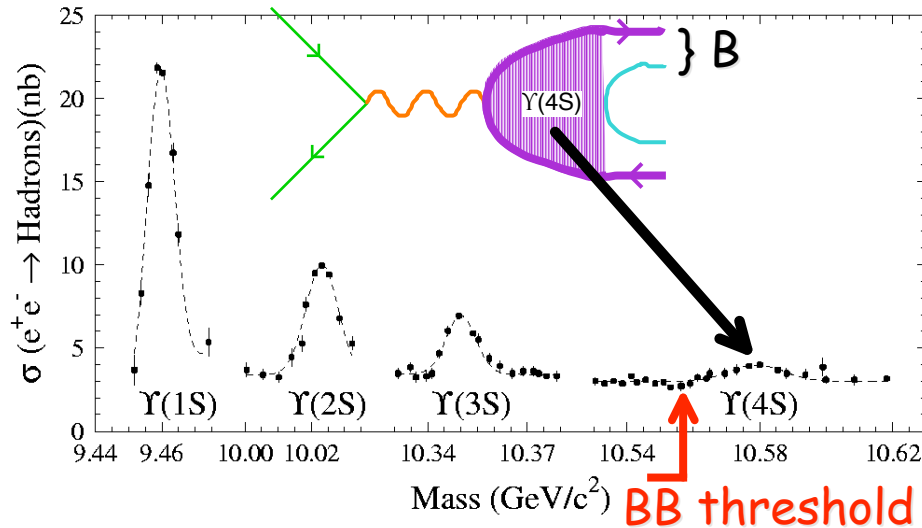
CP asymmetry from x-term(s) - no theoretical uncertainty: $\propto \arg(V_{td}^2) = 2\phi_1$

Bottom line: CP-dependent oscillation in time:

$$\frac{dN}{dt}(B \rightarrow f_{CP}) = \frac{1}{2}\Gamma e^{-\Gamma\Delta t} (1 + \eta_b \eta_{CP} \sin 2\phi_1 \sin(\Delta m \Delta t));$$

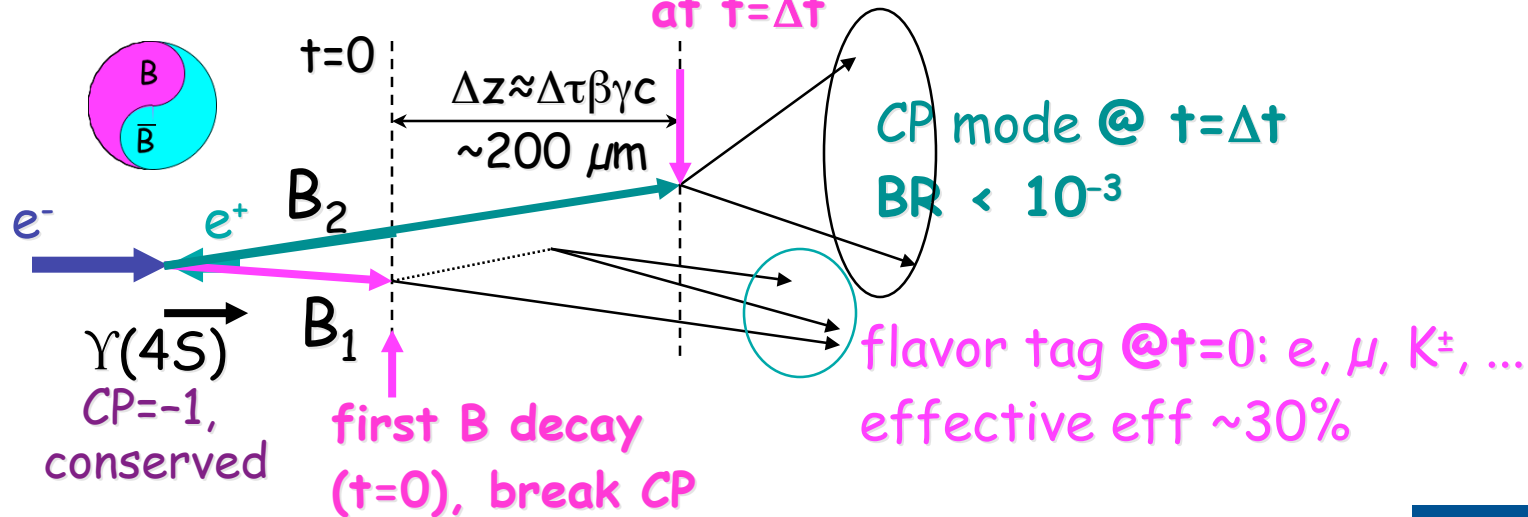
$$\eta_b = \begin{pmatrix} +1 & \text{if } B_{t=0} = B^0 \\ -1 & \text{if } B_{t=0} = \bar{B}^0 \end{pmatrix} \quad \eta_{CP} = \begin{pmatrix} -1 & \text{if } CP \text{ odd} \\ +1 & \text{if } CP \text{ even} \end{pmatrix}$$

B production: $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$

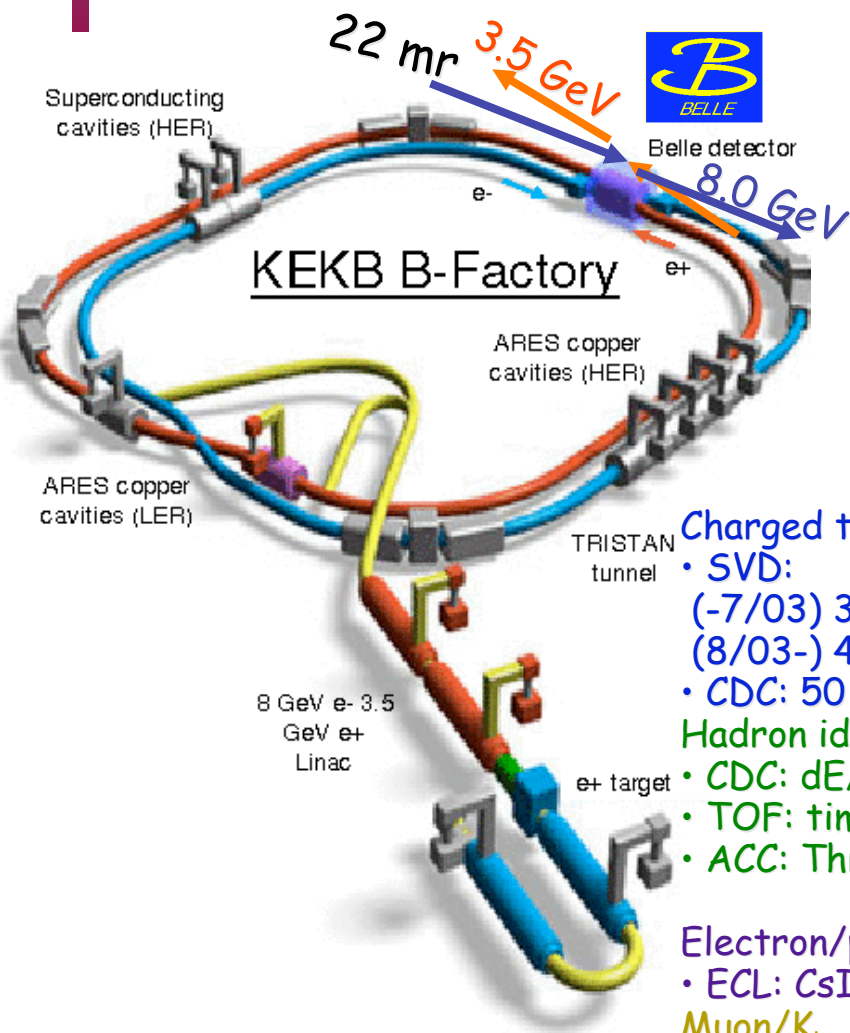


Δt by asymmetric energy $e^+e^- \rightarrow \Upsilon(4S)$
 (symmetric $\Upsilon(4S)$: CLEO 1979-2001)

Experimental design:
 hadron (K/π), lepton ID
 $\ll 200 \mu\text{m}$ vertexing
 statistics $\gg 10^7$ events



KEKB & Belle



- $L_{\max} = 1.53 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ (world record)
- Data (6/1999-4/2005)
- $\int L dt = 420 \text{ fb}^{-1} @ \{\Upsilon(4S) + \text{off}(\sim 10\%)\}$
- ($> 4.2 \times 10^8$ B events)

SVD1: 152M B pairs

SVD2: 123M+

Charged tracking/vertexing

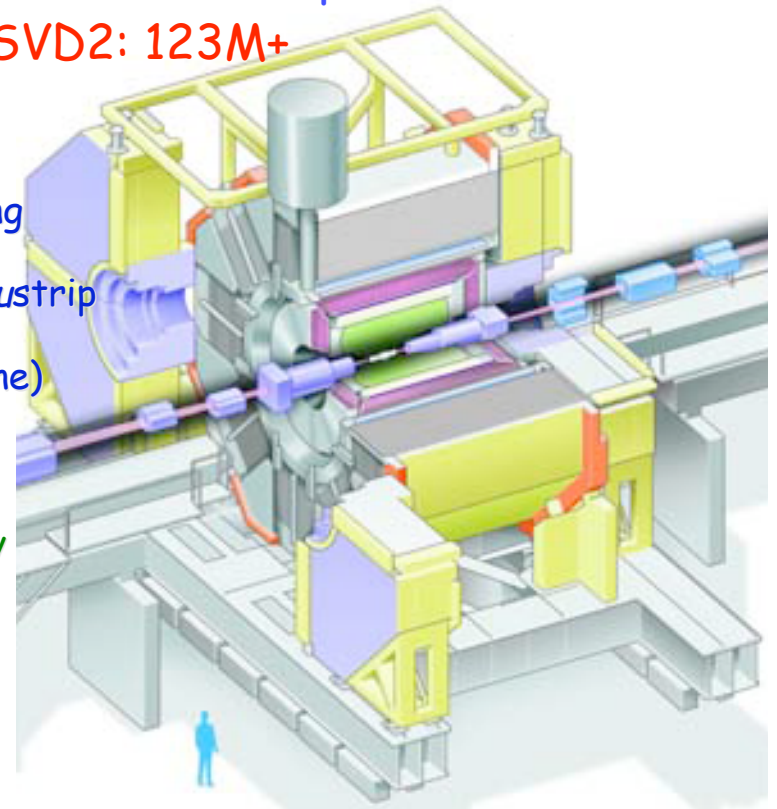
- SVD:
 - (-7/03) 3-layer DSSD Si μ strip
 - (8/03-) 4-layer
- CDC: 50 layers (He-ethane)

Hadron identification

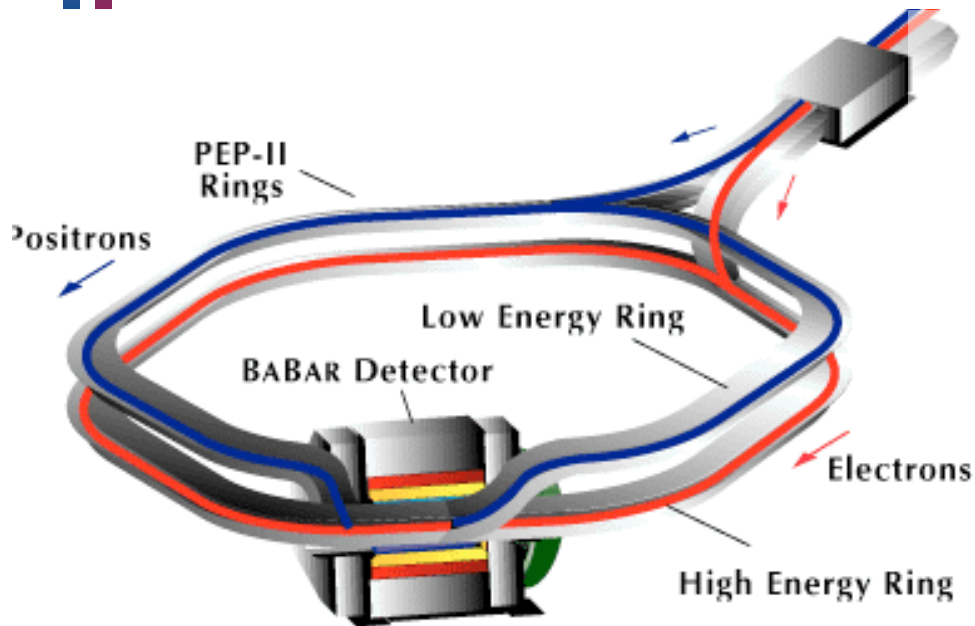
- CDC: dE/dx
- TOF: time-of-flight
- ACC: Threshold Cerenkov (aerogel)

Electron/photon

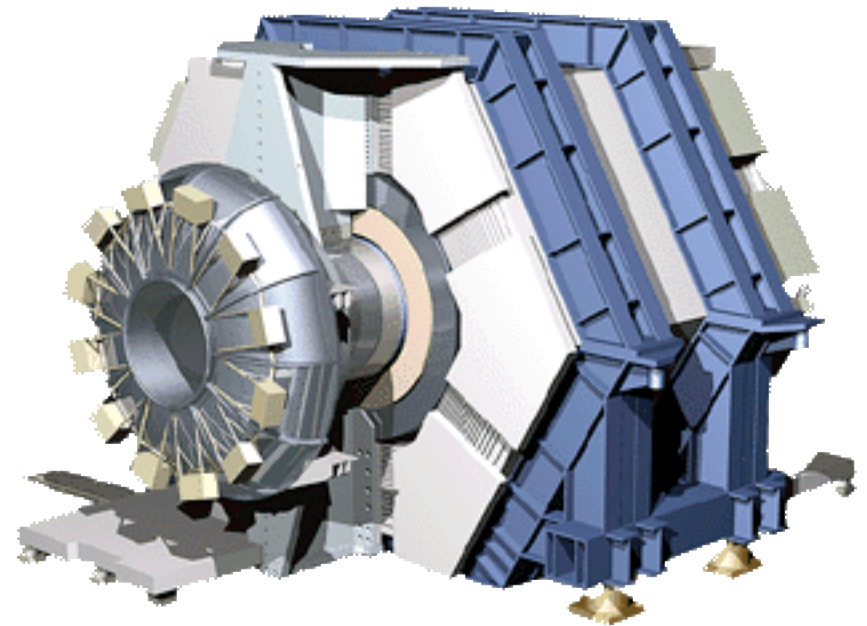
- ECL: CsI calorimeter
- Muon/ K_L
 - KLM: Resistive plate counter/iron



PEP-II & Babar



- $L_{\max} = 9.2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
- Data (1999-4/2005)
- $\int L dt = 250 \text{ fb}^{-1} @ \{\Upsilon(4S) + \text{off}(\sim 10\%)\}$
- ($> 2.5 \times 10^8$ B events)



- Charged tracking/vertexing
 - 5-layer DSSD Si μ strip
 - 40 layers (He-isobutane)
- Hadron identification
 - tracker: dE/dx
 - DIRC imaging Cerenkov
- Electron/photon
 - CsI calorimeter
- Muon/ K_L
 - Instrumented flux return

~11 nations, 80 institutes, ~650 persons

time-dependent CP analysis: overview

(Belle)

1) CP final state reconstruction exploit

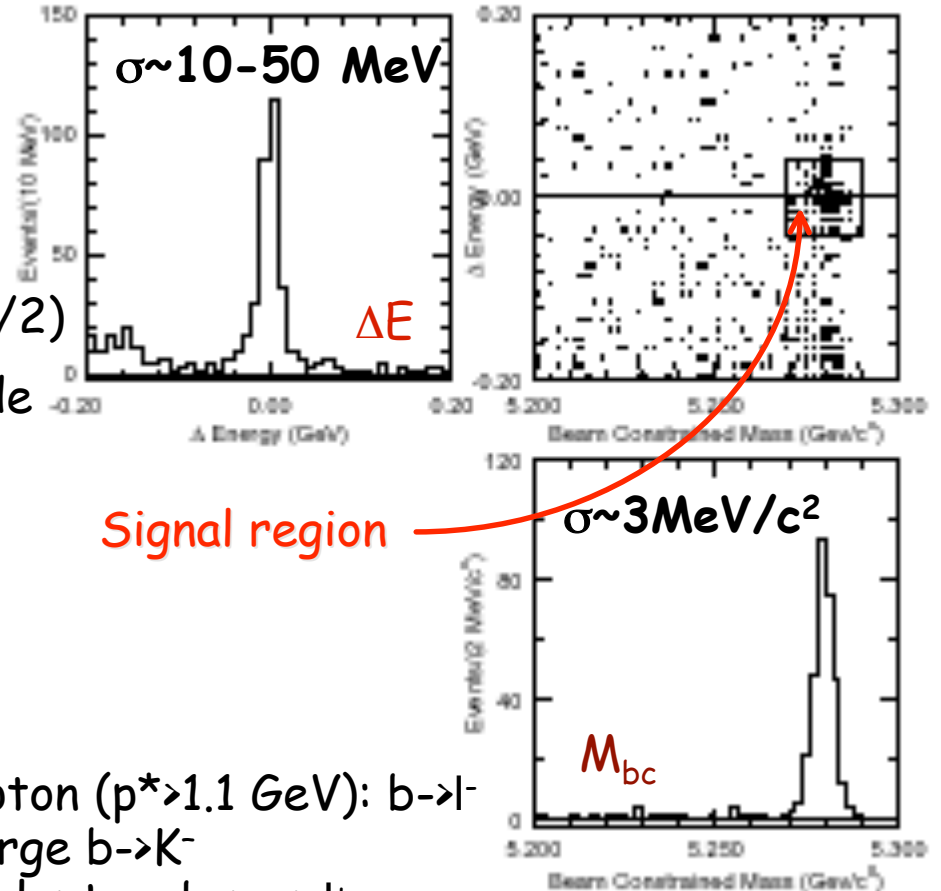
- exclusive pair production of B
- narrow resolution of collision energy

$$\Delta E = E_{\text{cand}}^* - E_{\text{beam}}^* = 0 \quad (E_{\text{beam}}^* = \sqrt{s}/2)$$

$\sigma \sim 10\text{-}50 \text{ MeV}$, depending on mode

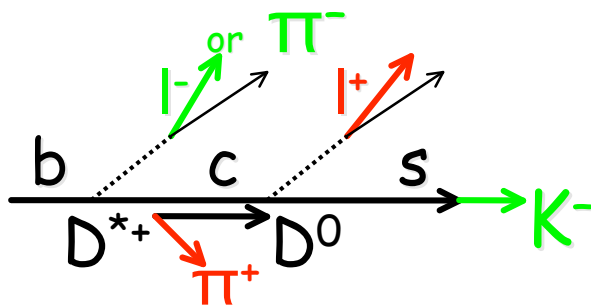
M_{bc} (Beam-constrained mass)

$$M_{bc} = (E_{\text{beam}}^{*2} - p_{\text{cand}}^{*2})^{1/2}$$



Signal region

2) Flavor tagging: sign of other b all remaining particles in the event



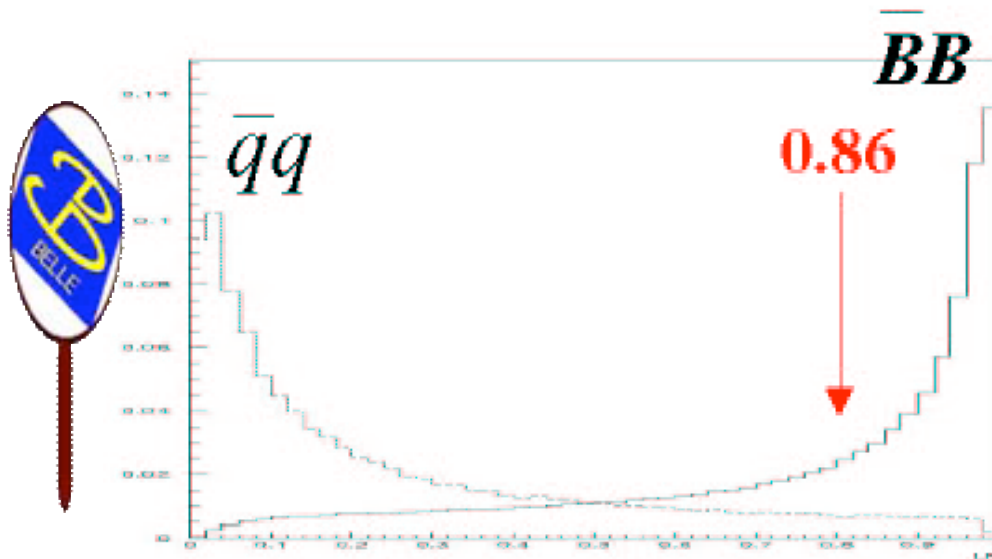
- high-p lepton ($p^* > 1.1 \text{ GeV}$): $b \rightarrow l^-$
- net K charge $b \rightarrow K^-$
- medium-p lepton, $b \rightarrow c \rightarrow l^+$
- soft π $b \rightarrow c \{D^{*+} \rightarrow D^0 \pi^+\}$
- hard π $b \rightarrow \{c\} \pi^- X$

multidimensional likelihood, $\epsilon > 99\%$

incorrect tag reduces ϵ , net $(28.7 \pm 0.5)\%$

time-dependent CP analysis: overview

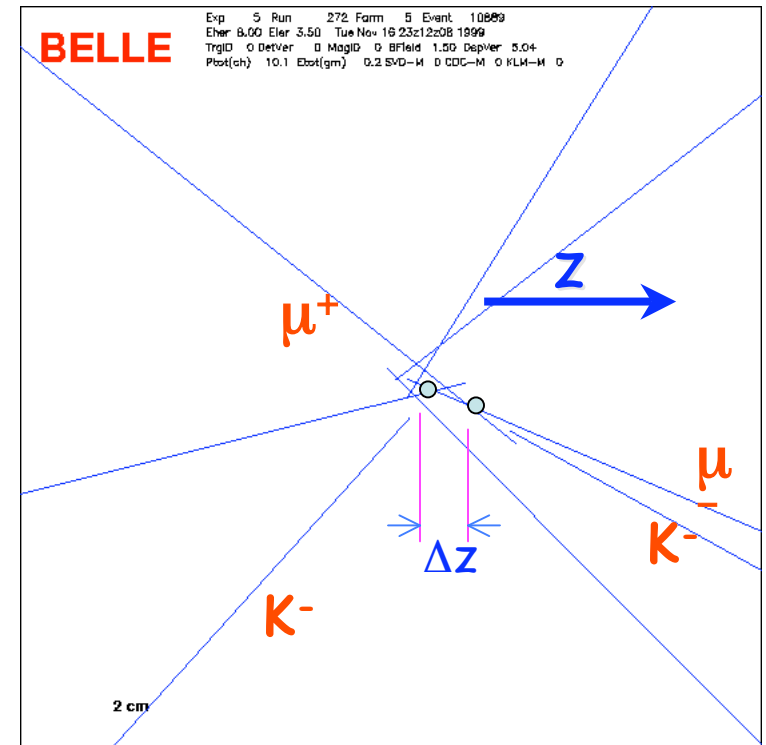
3) Continuum suppression:
event parameters ("shape")



$$R \equiv \frac{\mathcal{L}_{sig}}{\mathcal{L}_{sig} + \mathcal{L}_{bg}}$$

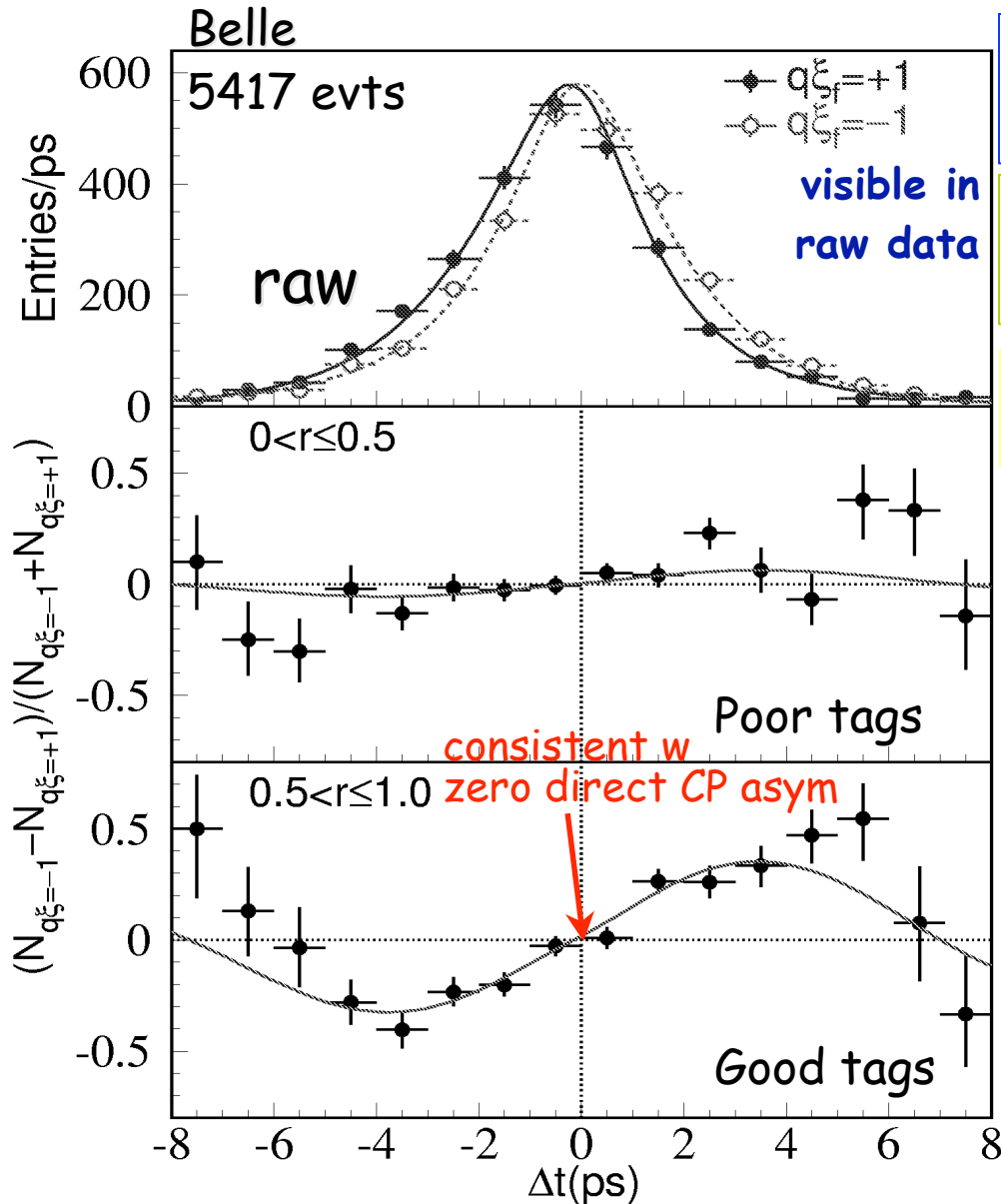
4) Vertex reconstruction

$$\Delta t \sim \Delta z / \beta \gamma c$$



5) Fit to Δt distribution:
unbinned maximum likelihood

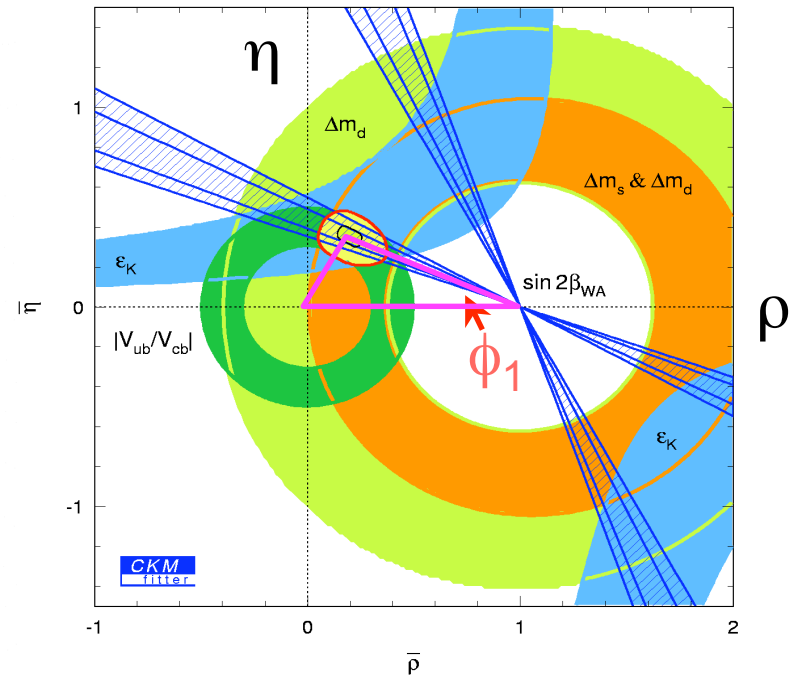
B → {Charmonium} + K^{(*)0} → sin 2φ₁



Belle 140 fb⁻¹ PRD71, 072003 (2005)
sin 2φ₁ = 0.728 ± 0.056 ± 0.023

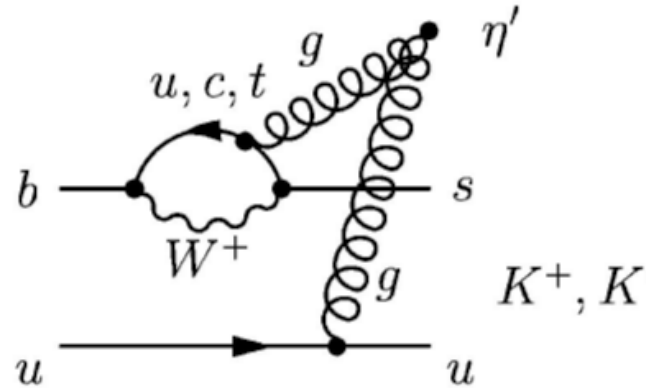
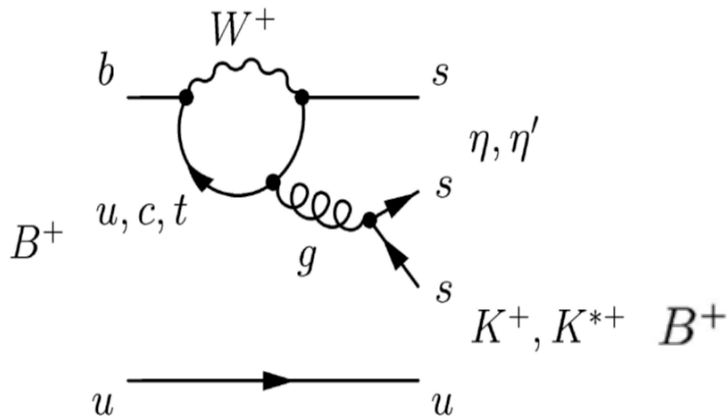
Babar 227 M evts hep-ex/0408127
sin 2φ₁ = 0.722 ± 0.040 ± 0.023

average:
sin 2φ₁ = 0.726 ± 0.037

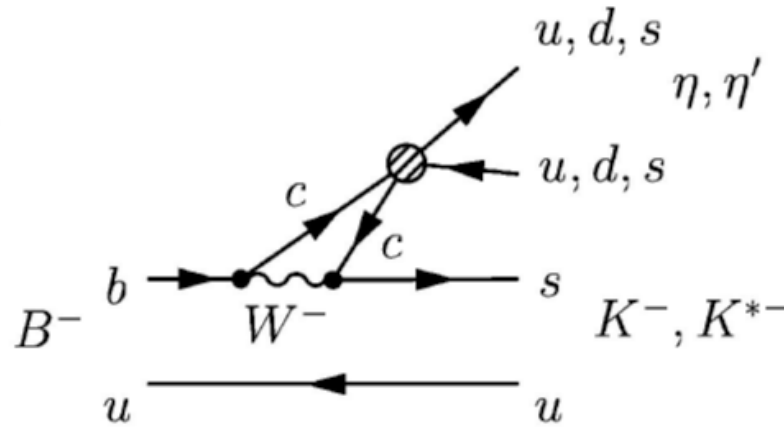
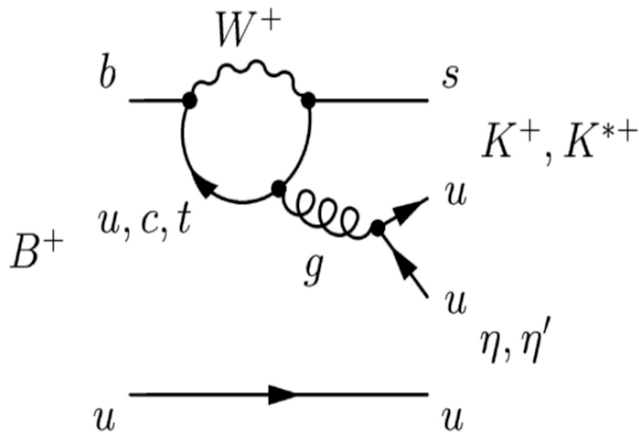
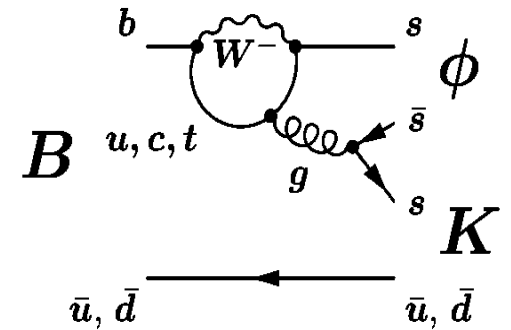


$\sin 2\phi_1$ in time-dependent $b \rightarrow s$ - or new physics?

modes dominated by $b \rightarrow sq\bar{q}$ penguins

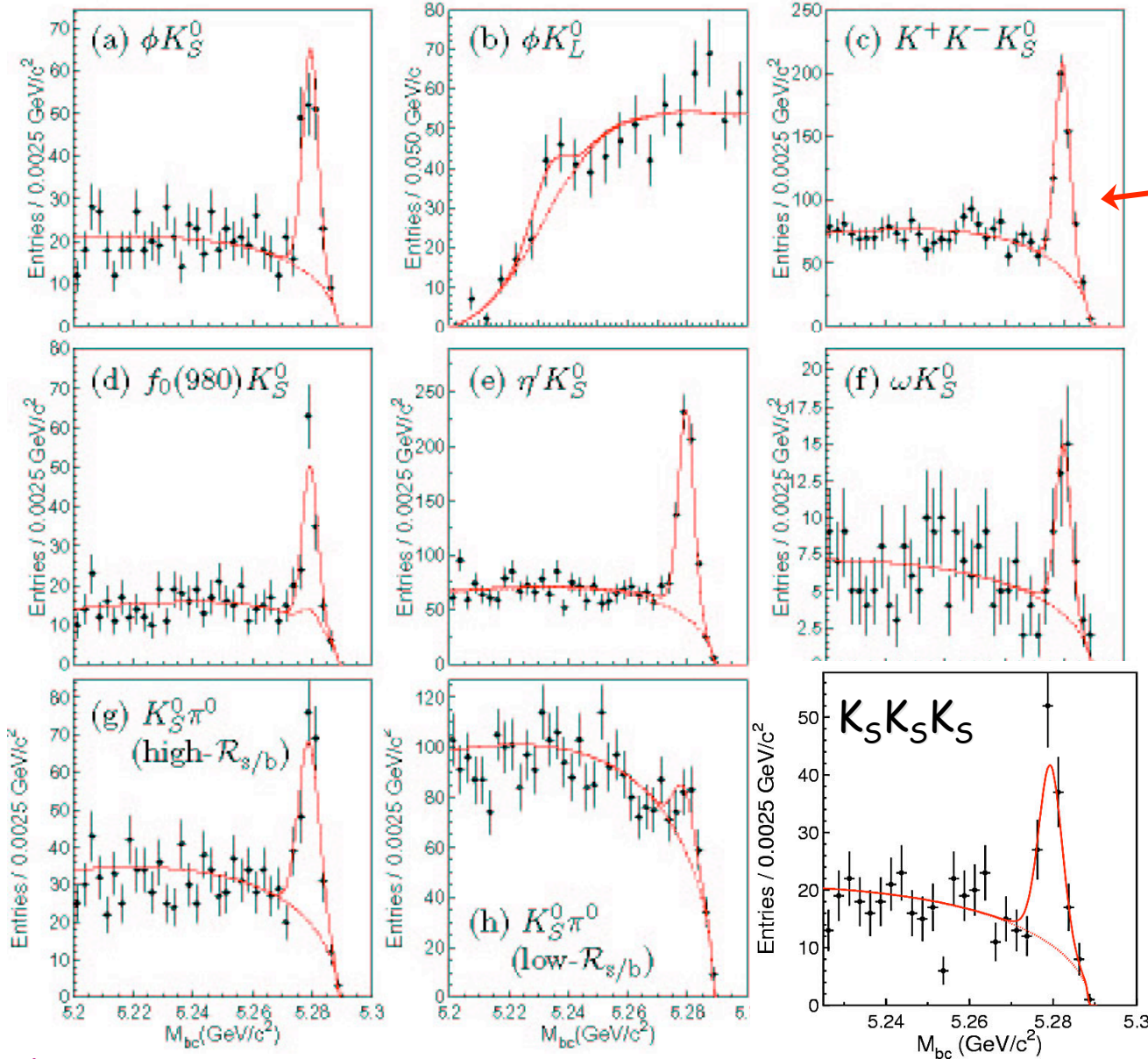


Theoretically cleanest



in the absence of New Physics, $S = \sin 2\phi_1$

Reconstruction of $b \rightarrow sqq$

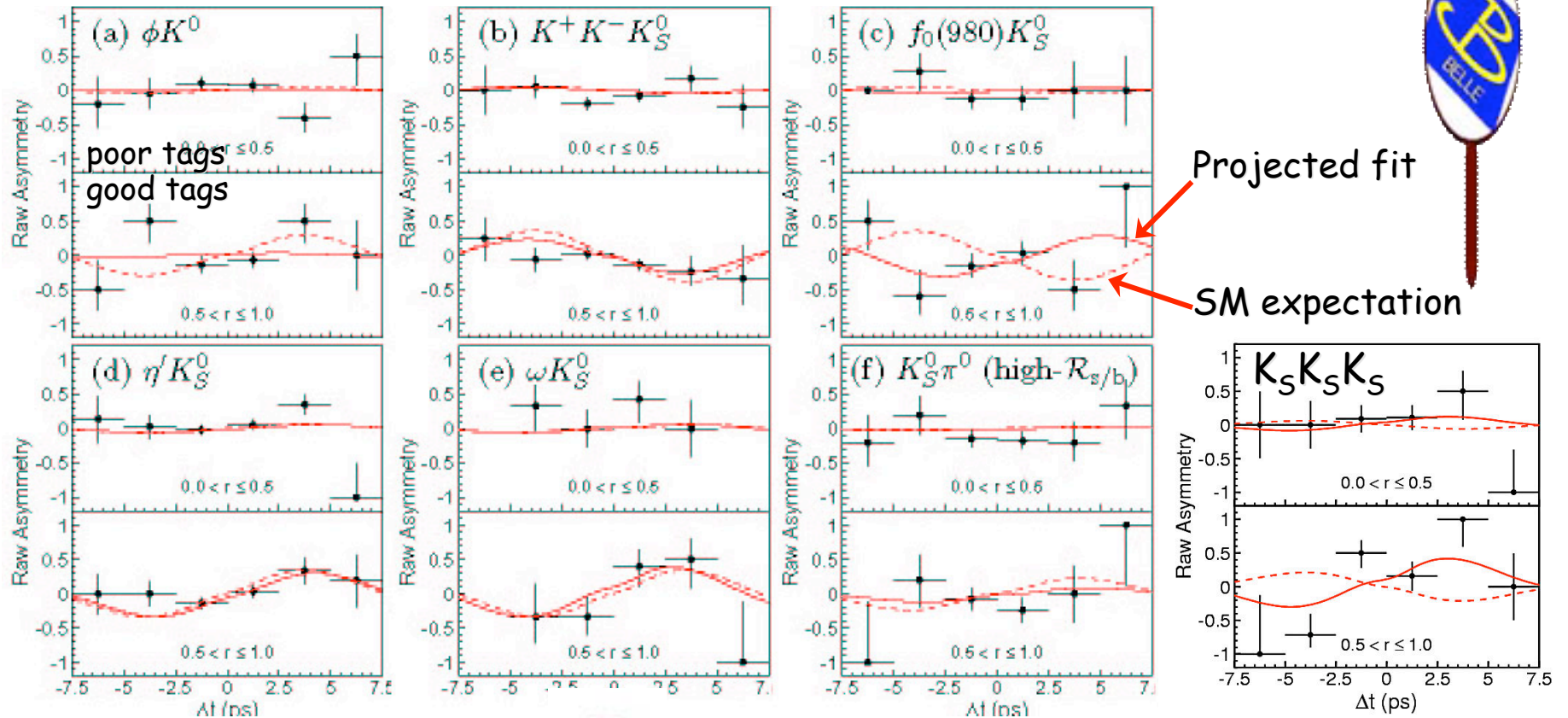


253 fb⁻¹

CP = +1
(angular analysis)



Time-dependent CP asymmetry:



(Belle)
[hep-ex/0409049](https://arxiv.org/abs/hep-ex/0409049)
[hep-ex/0503023](https://arxiv.org/abs/hep-ex/0503023)



(Babar)
[hep-ex/0408090](https://arxiv.org/abs/hep-ex/0408090)
[hep-ex/0408095](https://arxiv.org/abs/hep-ex/0408095)
[hep-ex/0502013](https://arxiv.org/abs/hep-ex/0502013)

[hep-ex/0502017](https://arxiv.org/abs/hep-ex/0502017)
[hep-ex/0502019](https://arxiv.org/abs/hep-ex/0502019)
[hep-ex/0503011](https://arxiv.org/abs/hep-ex/0503011)
[hep-ex/0503018](https://arxiv.org/abs/hep-ex/0503018)

Average "sin2φ₁" from b→s penguins

$$\sin 2\phi_1(b \rightarrow sq\bar{q}) =$$

$$\begin{cases} 0.39 \pm 0.11 \text{ (Belle)} \\ 0.45 \pm 0.09 \text{ (BABAR)} \end{cases}$$

World Average

$$\sin 2\phi_1(b \rightarrow sq\bar{q}) = 0.43 \pm 0.07$$

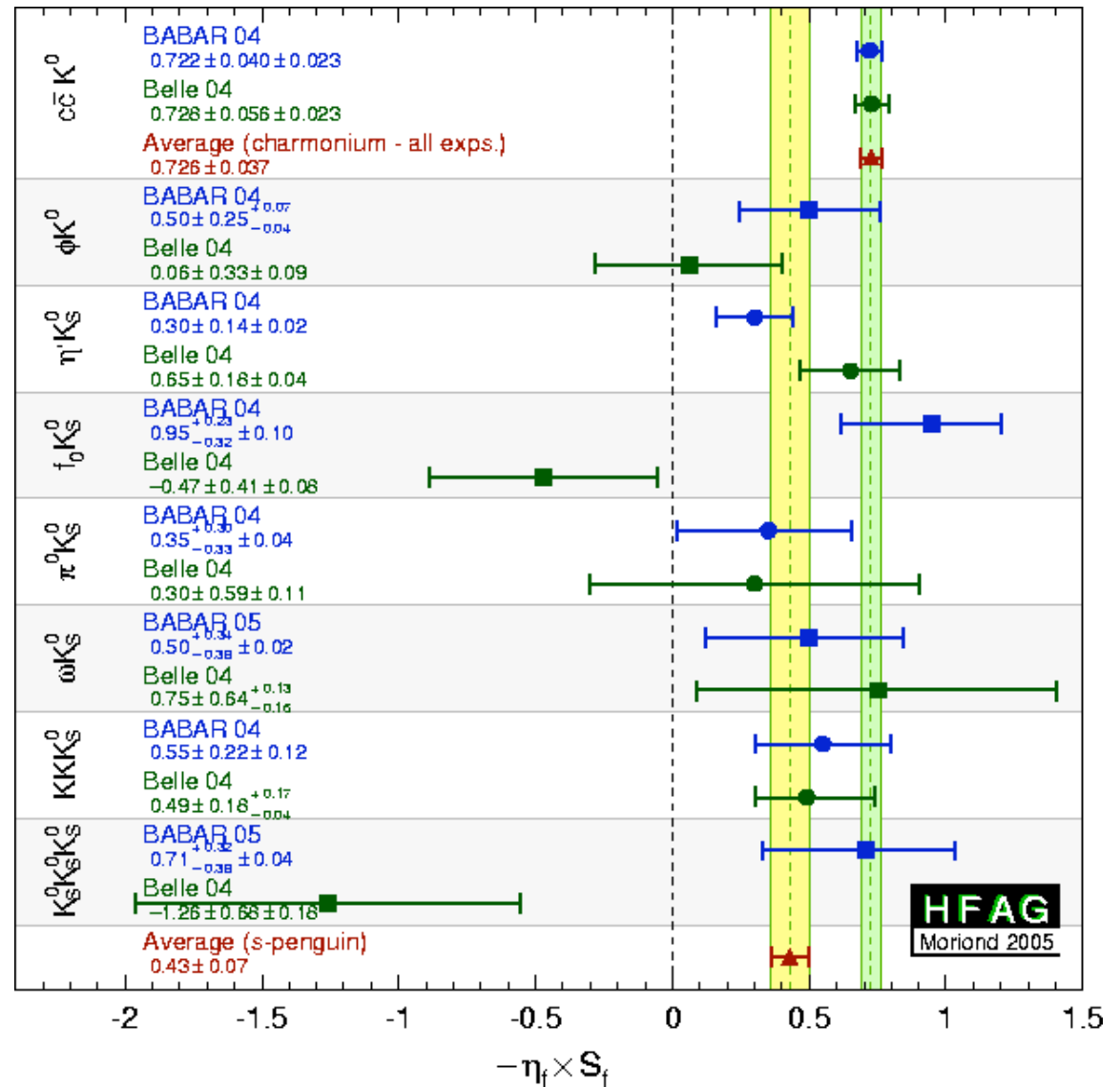
(excluding $K_S K_S K_S, f_0 K_S$)
 0.44 ± 0.08

Compare with $c\bar{c}s$:

$$\sin 2\phi_1(b \rightarrow c\bar{c}s) = 0.726 \pm 0.037$$

$$CL = 2.1 \times 10^{-4} \text{ (} 3.7\sigma \text{)}$$

- statistics?
- experimental systematics?
- theory corrections?
- new physics?



Average "sin2φ₁" from b→s penguins

$$\sin 2\phi_1(b \rightarrow sq\bar{q}) =$$

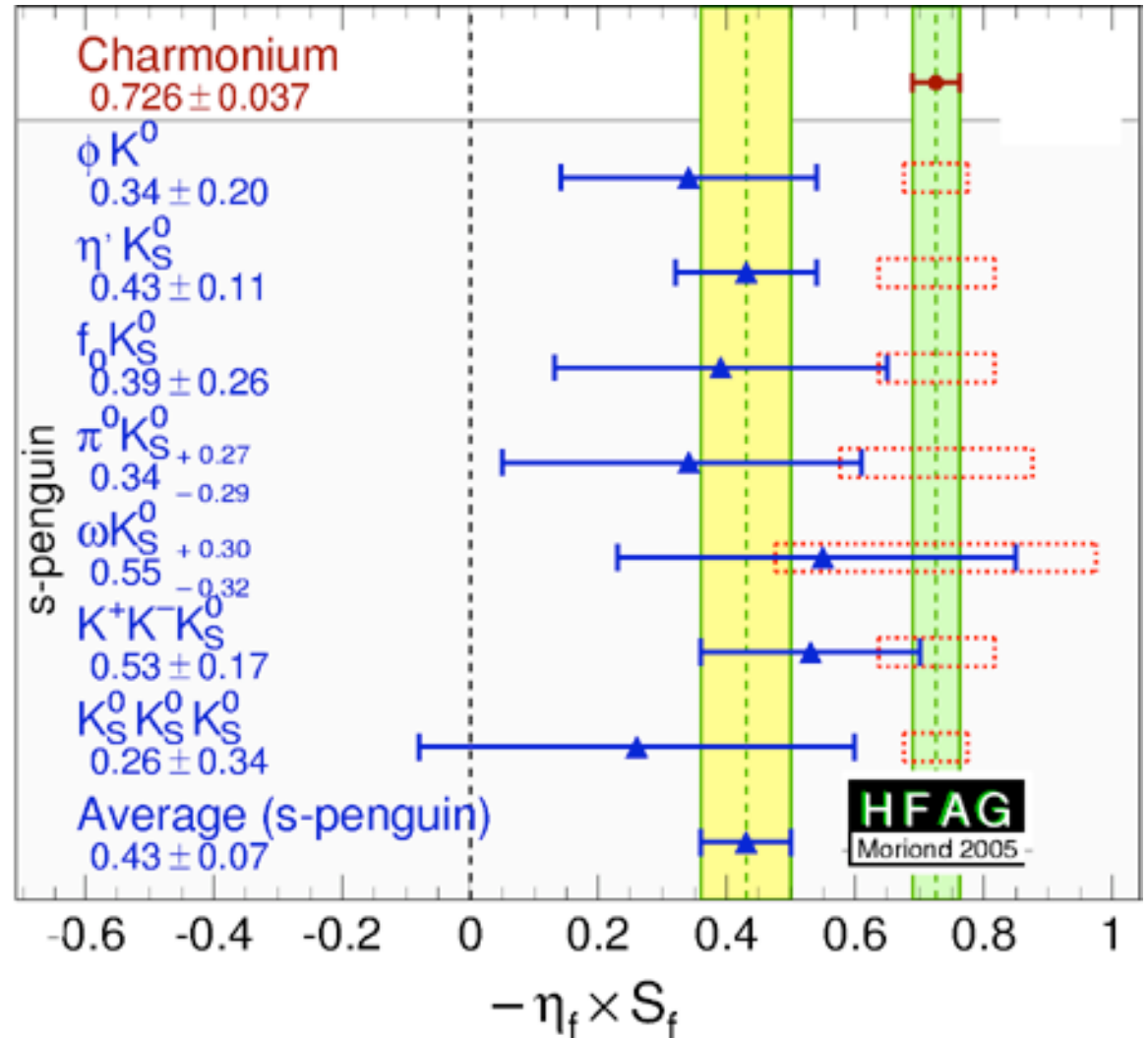
$$\begin{cases} 0.39 \pm 0.11 \text{ (Belle)} \\ 0.45 \pm 0.09 \text{ (BABAR)} \end{cases}$$

World Average
 $\sin 2\phi_1(b \rightarrow sq\bar{q}) = 0.43 \pm 0.07$

(excluding $K_S K_S K_S, f_0 K_S$)
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Compare with $c\bar{c}s$:
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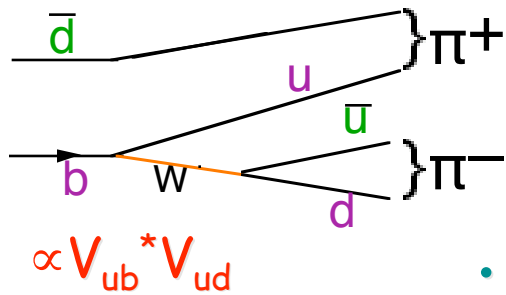
- statistics?
- experimental systematics?
- theory corrections?
- new physics?



$\sin 2\phi_2: B^0 \rightarrow \pi^+ \pi^-$

2 paths, each w/wo mixing:

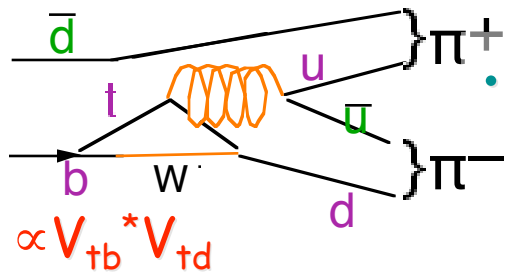
1) Tree (T)



+ with mixing

$$\propto V_{ub} V_{ud}^* \times V_{tb}^* V_{td}^2$$

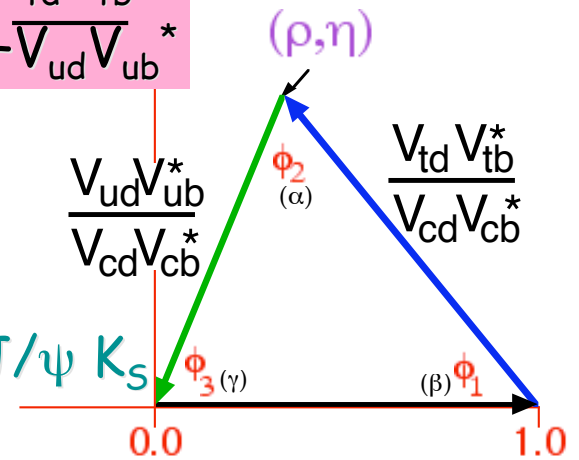
2) Penguin (P)



• if T dominates, $\rightarrow \sin 2\phi_2$, as w $J/\psi K_S$

• if P, T comparable, A_{CP} may include direct CP violation

$$\phi_2 = \arg \frac{V_{td} V_{tb}^*}{-V_{ud} V_{ub}^*}$$



$$q = \begin{cases} +1 & \text{if } B_{t=0} = B^0 \\ -1 & \text{if } B_{t=0} = \bar{B}^0 \end{cases}$$

$$\frac{dN}{dt}(B \rightarrow f_{CP}) = \frac{1}{2} \Gamma e^{-\Gamma \Delta t} (1 + q \cdot [\mathcal{A}_{\pi\pi} \cos(\Delta m \Delta t) + \mathcal{S}_{\pi\pi} \sin(\Delta m \Delta t)])$$

$$A_{\pi\pi} \neq 0, \mathcal{S}_{\pi\pi} \sim \sin(2\phi_2 + 2\theta) \cdot 2 / (|\lambda|^2 + 1)$$

difference of strong phase

$\neq 1$ if direct CP violation

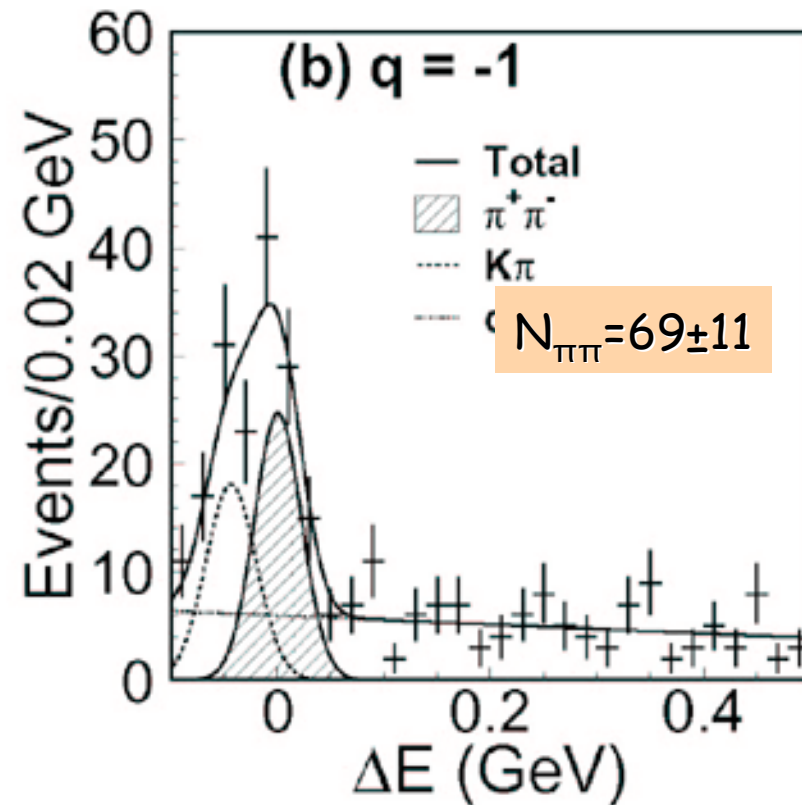
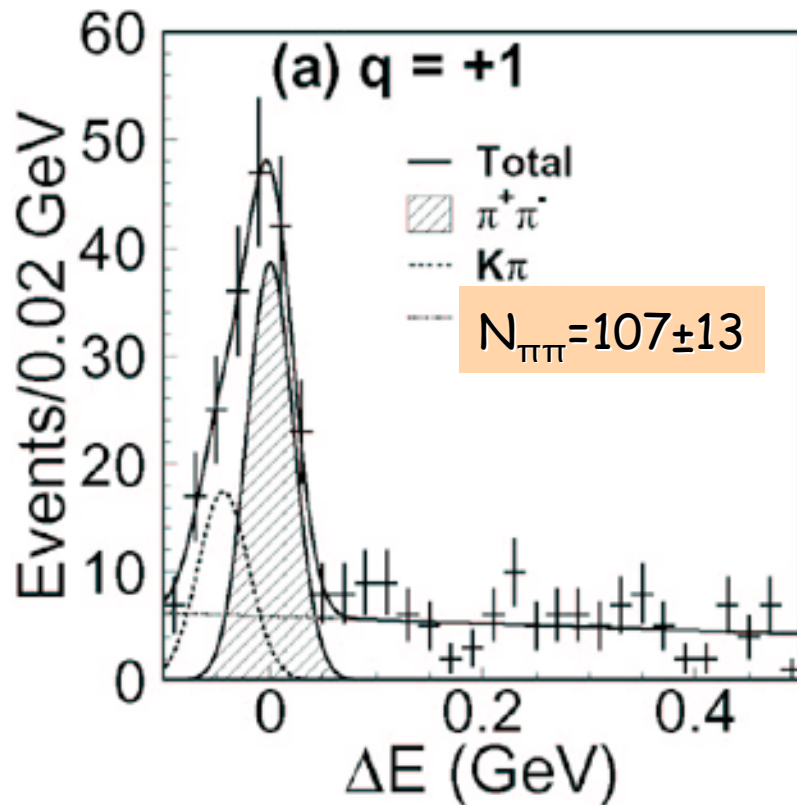
$\sin 2\phi_2: B^0 \rightarrow \pi^+ \pi^-$

An observable time-integrated asymmetry

hep-ex/0502035

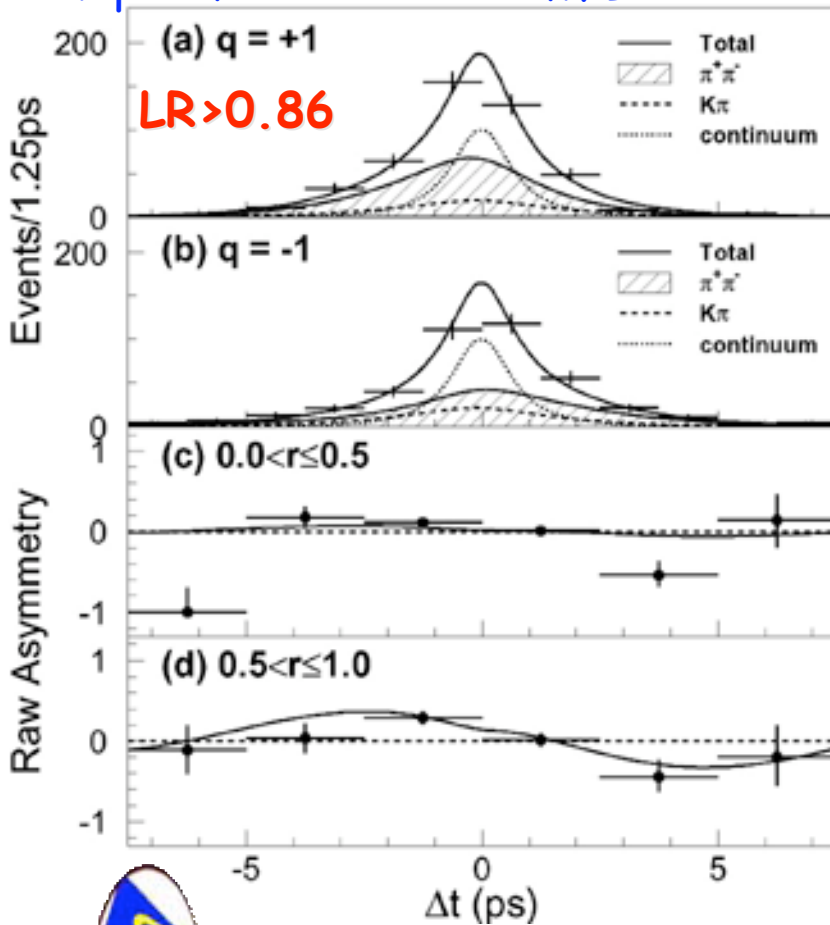


High quality tags ($LR > 0.86, 0.5 < r < 1.0$)



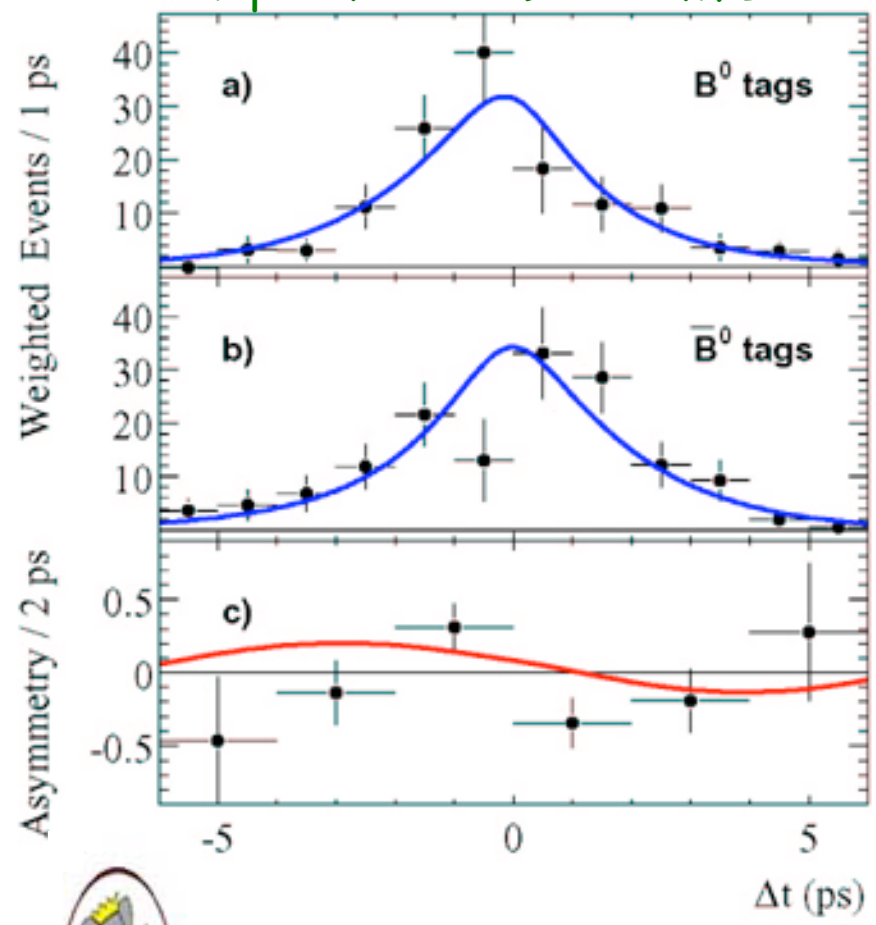
$\sin 2\phi_2: B^0 \rightarrow \pi^+ \pi^-$

hep-ex/0502035 275M B evts



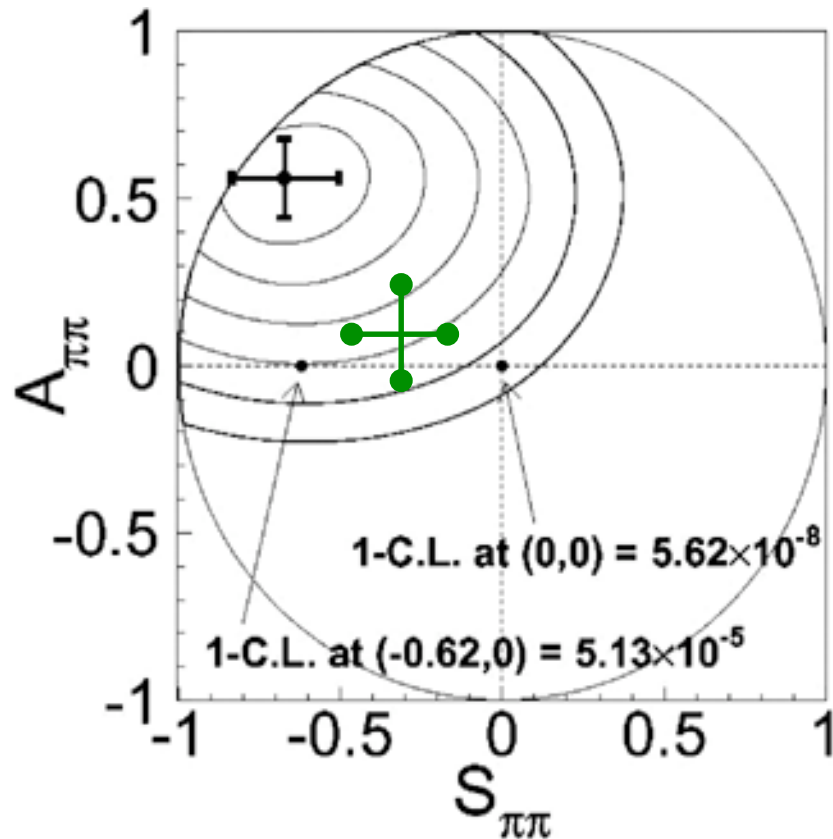
$A = +0.58 \pm 0.12 \pm 0.06$
 $S = -0.67 \pm 0.16 \pm 0.06$

hep-ex/0408090 227M B evts



$-A=C = -0.09 \pm 0.15 \pm 0.04$
 $S = -0.30 \pm 0.17 \pm 0.03$

$\sin 2\phi_2: B^0 \rightarrow \pi^+\pi^-$

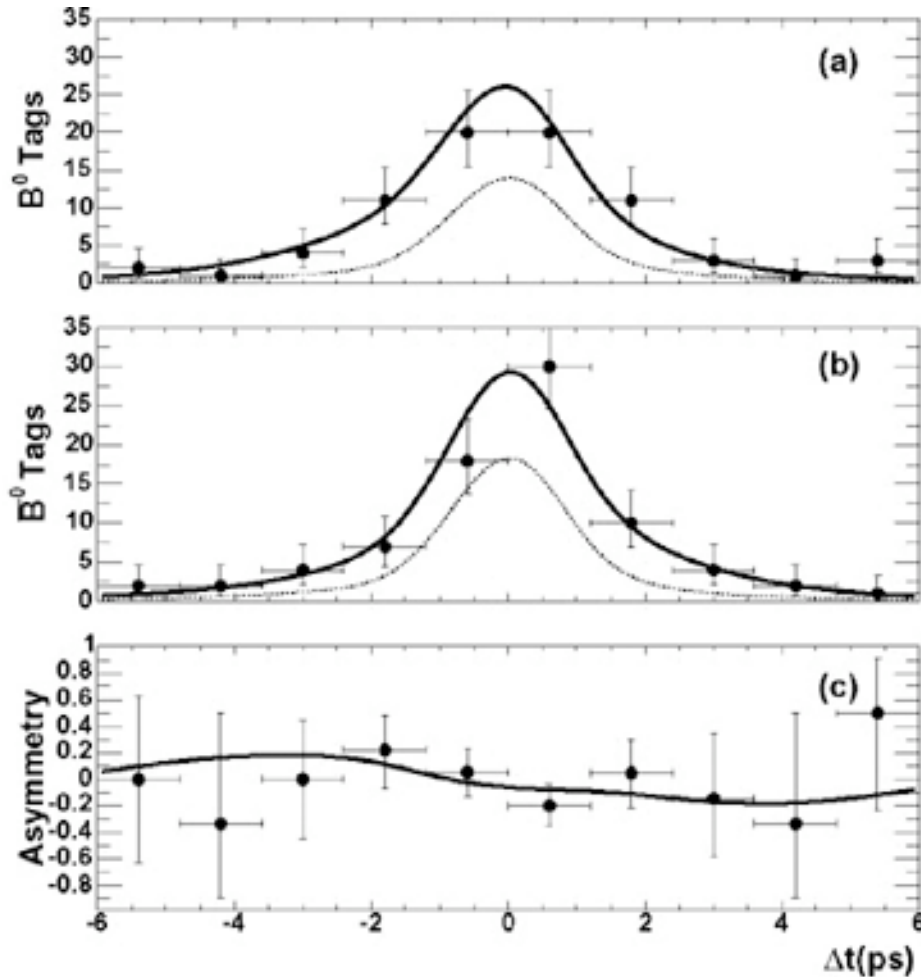


Validation of results

- lifetime
- sidebands
- $K\pi$ lifetime, mixing, CP asymmetry
- many subsamples - consistent results
- time-integrated asymmetry
- statistics - ensemble simulation study

$\sin 2\phi_2: B^0 \rightarrow \rho^+\rho^-$

hep-ex/0505049 232M B evts



CP depends on polarization

Longitudinal: CP = +1

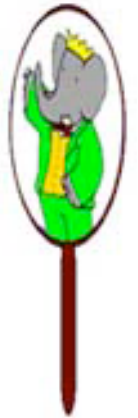
Transverse: CP mixed

CP fit includes helicity:

$$f_L = 0.978 \pm 0.014^{+0.021}_{-0.029}$$

$$S_L = -0.33 \pm 0.24^{+0.08}_{-0.14}$$

$$C_L = -0.03 \pm 0.18 \pm 0.09$$



Constraints on ϕ_2

Gronau & Rosner, PRD 65, 093012 (2002)

$$A(B^0 \rightarrow \pi^+ \pi^-) = -(|T|e^{i\delta_T} e^{i\phi_2} + |P|e^{i\delta_P})$$

$$A(\bar{B}^0 \rightarrow \pi^+ \pi^-) = -(|T|e^{i\delta_T} e^{-i\phi_2} + |P|e^{i\delta_P})$$
$$\delta \equiv \delta_P - \delta_T$$

$$A_{\pi\pi} = \frac{-2|P/T| \sin(\phi_1 + \phi_2) \sin \delta}{1 - 2|P/T| \cos(\phi_1 + \phi_2) \cos \delta + |P/T|^2}$$

$$S_{\pi\pi} = \frac{2|P/T| \sin(\phi_1 - \phi_2) \cos \delta + \sin 2\phi_2 - |P/T|^2 \sin 2\phi_1}{1 - 2|P/T| \cos(\phi_1 + \phi_2) \cos \delta + |P/T|^2}$$

Known: $\sin 2\phi_1 = 0.726 \pm 0.037$

Unknown: $|P/T|, \delta, \phi_2$

New constraints: $A, S \rightarrow \phi_2$ not fully constrained (CL contours)

ϕ_2 : isospin relations

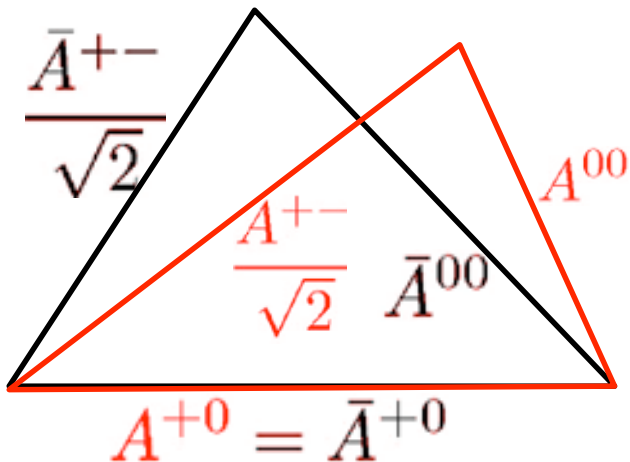
Gronau & London, PRL 65, 3381 (1990)

Isospin-related final states, different T, P content :

$$\frac{A(B^0 \rightarrow \pi^+ \pi^-)}{\sqrt{2}} + A(B^0 \rightarrow \pi^0 \pi^0) = A(B^+ \rightarrow \pi^+ \pi^0)$$

$$\frac{A(\bar{B}^0 \rightarrow \pi^+ \pi^-)}{\sqrt{2}} + A(\bar{B}^0 \rightarrow \pi^0 \pi^0) = A(\bar{B}^- \rightarrow \pi^- \pi^0)$$

|| (pure T)



-> solve & disentangle:

$$\mathcal{B}(B^0 \rightarrow \pi^+ \pi^-)$$

$$\mathcal{B}(B^0 \rightarrow \pi^0 \pi^0)$$

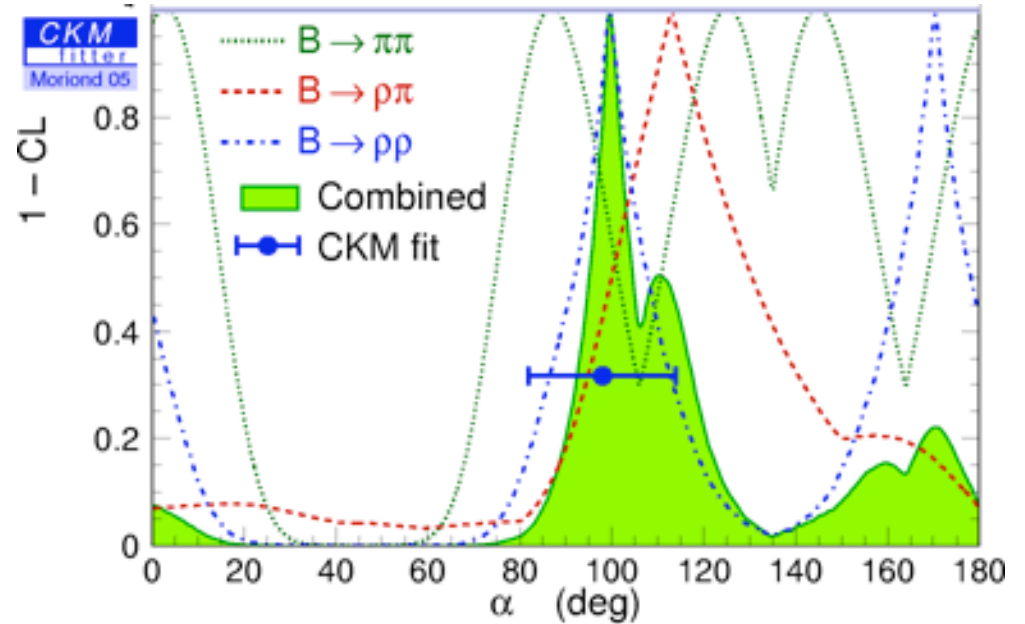
$$\mathcal{B}(B^+ \rightarrow \pi^+ \pi^0)$$

+ $\pi^+ \pi^-, \pi^0 \pi^0$ CP asymmetries

Also applies to $\rho\rho$

ϕ_2 : isospin relations

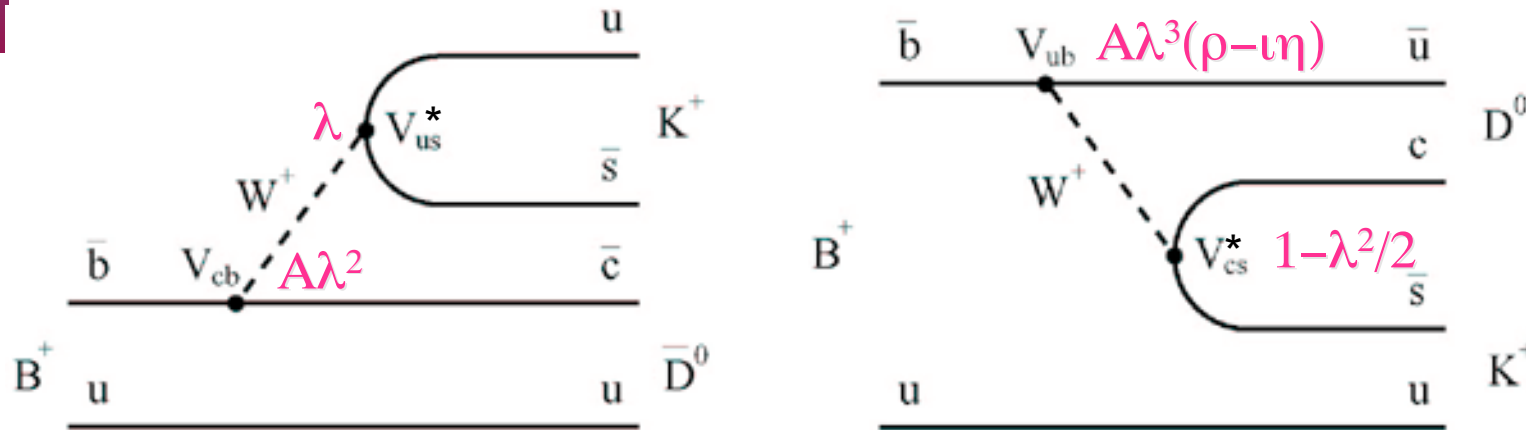
χ^2 analysis to constrain ϕ_2
(hep-ph/0406184)



	$\mathcal{B}_{+-}(10^{-6})$	$\mathcal{B}_{+0}(10^{-6})$	$\mathcal{B}_{00}(10^{-6})$	\mathcal{A}_{00}	ϕ_2
$\pi\pi$					
Belle	$4.4 \pm 0.6 \pm 0.3$	$5.0 \pm 1.2 \pm 0.5$	$2.32^{+0.44}_{-0.48} \quad ^{+0.22}_{-0.18}$	$0.43 \pm 0.51^{+0.17}_{-0.16}$	$[71^\circ, 180^\circ]$ (95.4% CL)
Babar	$4.7 \pm 0.6 \pm 0.2$	$5.8 \pm 0.6 \pm 0.4$	$1.17 \pm 0.32 \pm 0.10$	$0.12 \pm 0.56 \pm 0.06$	$[61^\circ, 180^\circ]$ (90% CL)
$\rho\rho$					
Babar	$30 \pm 4 \pm 5$	$22.5^{+5.7}_{-5.4} \pm 5.8$	$< 1.1(90\%CL)$	-	$[79^\circ, 123^\circ]$ (90% CL)

ϕ_3 :

A. Bondar, Belle internal (2003)
 Giri et al, PRD 68, 054018 (2003)



$$A(B^+ \rightarrow D^0 K^+) = r e^{i(\delta - \phi_3)} A(B^+ \rightarrow \bar{D}^0 K^+) \quad (r \sim 0.1 - 0.2)$$

IF $D^0, \bar{D}^0 \rightarrow K_S \pi^+ \pi^-$: $m_+ \equiv m_{K_S \pi^+}$ $m_- \equiv m_{K_S \pi^-}$

$$A(\bar{D}^0 \rightarrow K_S \pi^+ \pi^-) = f(m_+^2, m_-^2) \rightarrow A(D^0 \rightarrow K_S \pi^+ \pi^-) = f(m_-^2, m_+^2)$$

$$M_+ = A(B^+ \rightarrow \bar{D}^0 K^+) [f(m_+^2, m_-^2) + r e^{i(\delta - \phi_3)} f(m_-^2, m_+^2)]$$

$$M_- = A(B^+ \rightarrow D^0 K^+) [f(m_-^2, m_+^2) + r e^{i(\delta + \phi_3)} f(m_+^2, m_-^2)]$$

$f(m_+^2, m_-^2)$ from continuum D^0

ϕ_3 :

Belle: hep-ex/0411049 253 fb⁻¹

Babar: hep-ex/0504039 227 M B evts

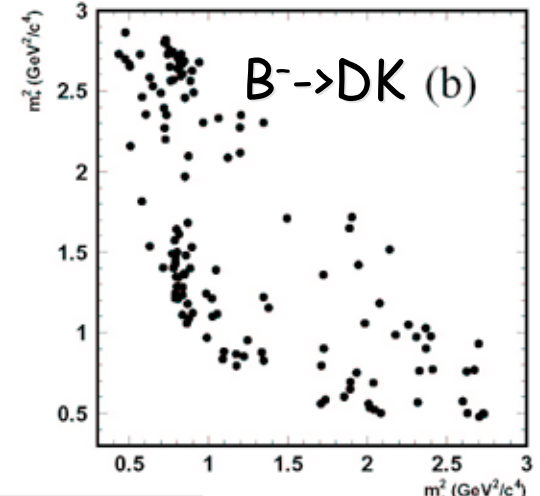
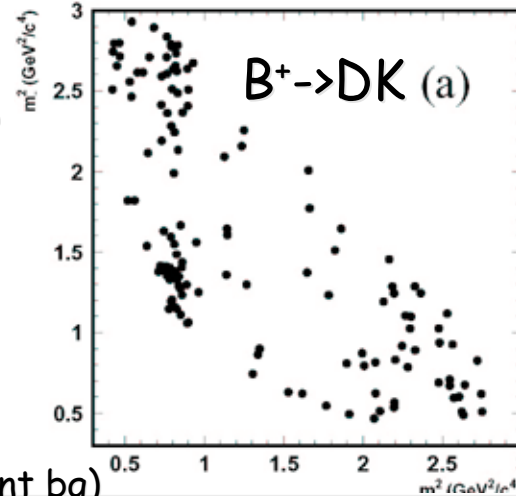
Dalitz plots -
unbinned ML fit for ϕ_3, δ, r

Results for

$B \rightarrow DK$

$B \rightarrow D^* K$

$B \rightarrow DK^* (K^* \rightarrow K_S \pi^+)$



$\chi + (\text{stat}) + (\text{sys}) + (\text{D model}) + (\text{nonresonant bg})$

	r	$\phi_3(^{\circ})$	$\delta(^{\circ})$
<i>DK</i>			
Belle	$0.21 \pm 0.08 \pm 0.03 \pm 0.04$	$64 \pm 19 \pm 13 \pm 11$	$157 \pm 19 \pm 11 \pm 21$
Babar	< 0.19 (90%CL)	$70 \pm 44 \pm 10 \pm 10$	$114 \pm 41 \pm 8 \pm 10$
<i>D*⁰K</i>			
Belle	$0.12^{+0.16}_{-0.11} \pm 0.02 \pm 0.04$	$75 \pm 57 \pm 11 \pm 11$	$321 \pm 57 \pm 11 \pm 21$
Babar	$0.155 \pm^{+0.070}_{-0.077} \pm 0.040 \pm 0.020$	$73 \pm 35 \pm 10 \pm 10$	$303 \pm 34 \pm 14 \pm 10$
<i>DK*</i>			
Belle	$0.25^{+0.17}_{-0.18} \pm 0.09 \pm 0.04 \pm 0.08$	$112 \pm 35 \pm 9 \pm 11 \pm 8$	$353 \pm 35 \pm 8 \pm 21 \pm 49$

Belle average

(excl DK*):

$(68 \pm 15 \pm 13 \pm 11)^{\circ}$

Babar average:

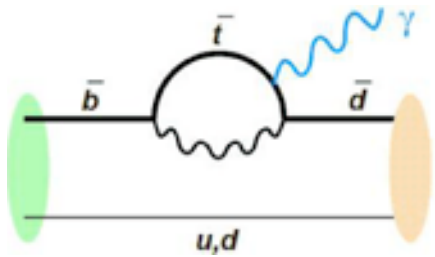
$(70 \pm 26 \pm 10 \pm 10)^{\circ}$

$|V_{td}/V_{ts}|: b \rightarrow d\gamma / b \rightarrow s\gamma$

Belle: hep-ex/0408137

Babar: PRL 94, 011801 (2005)

Ratio \rightarrow smaller theory error $\sim 10\%$



274 M B evts (1.9σ)

$|V_{td}/V_{ts}| < 0.21$ (90% CL)



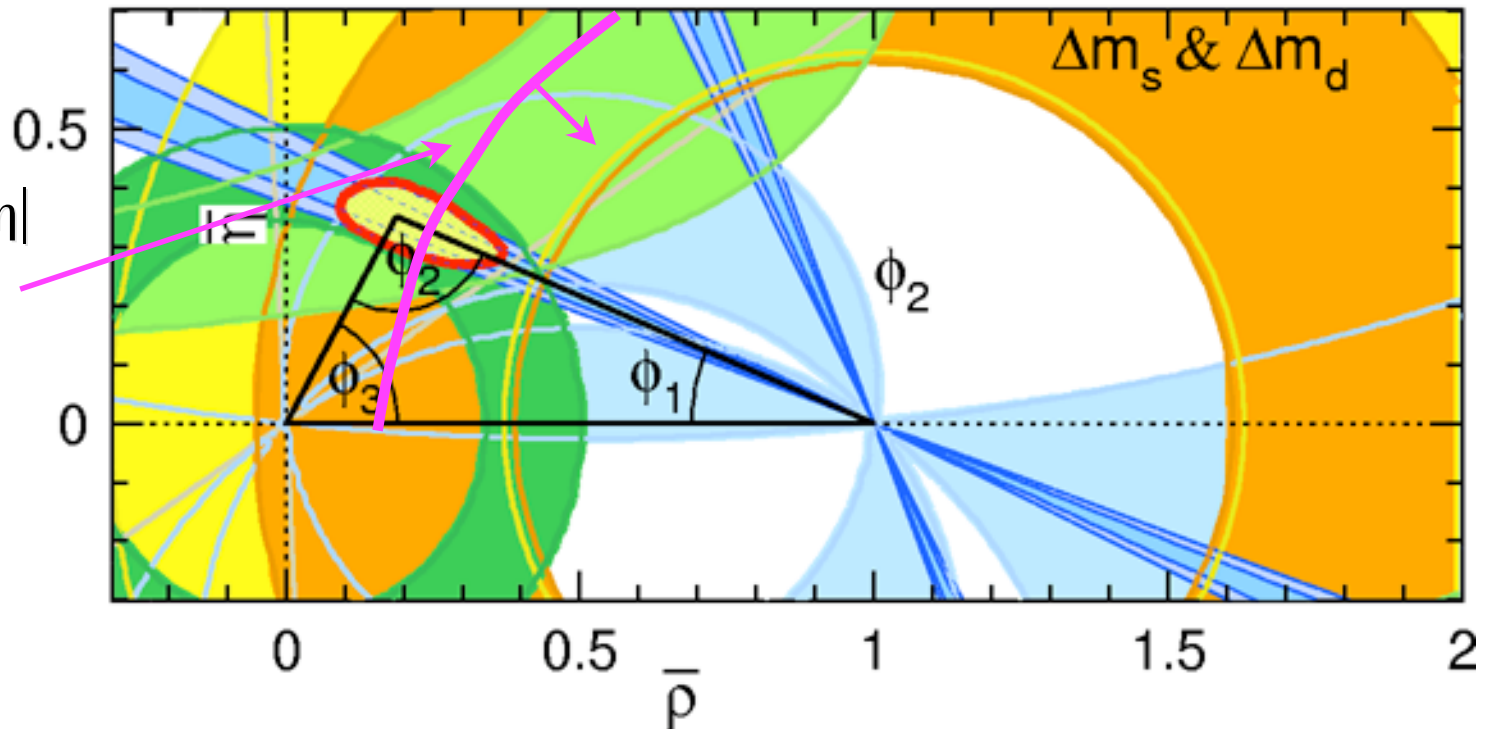
221 M B evts (2.1σ)

$|V_{td}/V_{ts}| < 0.19$ (90% CL)

$$|V_{td}/V_{ts}| = \lambda |1 - \rho - i\eta|$$

$$\Rightarrow |1 - \rho - i\eta| < 0.86$$

(90% CL)



Summary

B Factories 1999-2005:

- Total $> 6.5 \times 10^8$ B pairs, results on $\sim 5 \times 10^8$
- $\sin 2\phi_1$ via $\psi K^{(*)0}$ to $\pm 5\%$
- alternative probes of $\sin 2\phi_1$ - sensitive to new physics
penguin-dominated B \rightarrow sqq - suggestive!
- $\sin 2\phi_2$ - direct CP violation, π/ρ modes $\rightarrow \pm 20^\circ$
- ϕ_3 : first constraints $\rightarrow \pm 20^\circ$
- possible hints of $b \rightarrow d\gamma$ (+ other CKM) \rightarrow
higher precision on sides

Next

- summer 2005 $> 450 \text{ fb}^{-1}$ Belle, $> 300 \text{ fb}^{-1}$ Babar
- multiple modes, techniques
- \rightarrow improving precision on angles and sides;
CKM challenge is heating up - stay tuned!