

What is Linear Algebra?

Linear Algebra
MATH 2076



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Systems of Linear Equations and their Solutions

A *system* of linear equation in “unknowns” (the *variables*) x_1, x_2, \dots, x_n has the form

$$a_{11}x_1 + a_{12}x_2 + \cdots + a_{1n}x_n = b_1$$

$$a_{21}x_1 + a_{22}x_2 + \cdots + a_{2n}x_n = b_2$$

$$\vdots \quad \quad \quad \vdots \quad \quad \quad \vdots \quad \quad \quad \vdots$$

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A *solution* to the above system is a list (s_1, s_2, \dots, s_n) of numbers such that setting $x_1 = s_1, \dots, x_n = s_n$ makes **all** of the equations true statements. The *solution set* consists of **all** solutions.